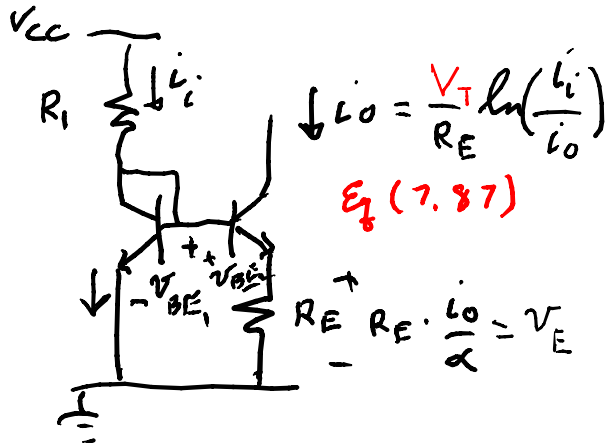


Homework due W
Exam next M

P.544 = Widlar current mirror



$$I_i = \frac{1}{\alpha} \cdot I_{SE} e^{V_{BE1}/V_T}$$

$$I_o = \frac{1}{\alpha} \cdot I_{SE} e^{V_{BE2}/V_T}$$

$$V_{BE1} = V_T \ln\left(\frac{I_i \cdot \alpha}{I_{SE}}\right)$$

$$V_{BE2} = V_T \ln\left(\frac{I_o \cdot \alpha}{I_{SE}}\right)$$

$$V_{BE1} = V_{BE2} + \frac{R_E}{\alpha} I_o$$

$$V_{BE1} - V_{BE2} = V_T \ln\left(\frac{I_i}{I_o}\right) = \frac{R_E}{\alpha} I_o \Rightarrow I_o = \frac{\alpha V_T}{R_E} \ln\left(\frac{I_i}{I_o}\right)$$

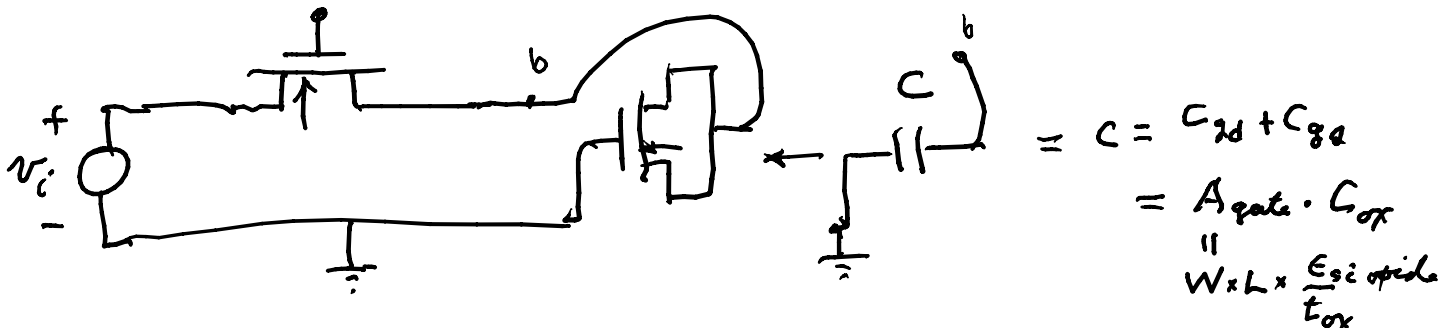
Without R_E , $R_E = 0$; $V_{CC} = R_1 I_i + 0.7$ with $R_E \neq 0$ can raise I_i for the same I_o

$$\text{If } R_E = 0 \quad 0 = \alpha V_T \ln(I_i/I_o) \Rightarrow I_o/I_i = 1$$

means R_1 can be smaller as still $I_i = (V_{CC} - 0.7)/R_1$

\Rightarrow better for VLSI where we desire smaller resistors

Pass transistor, p. 1155

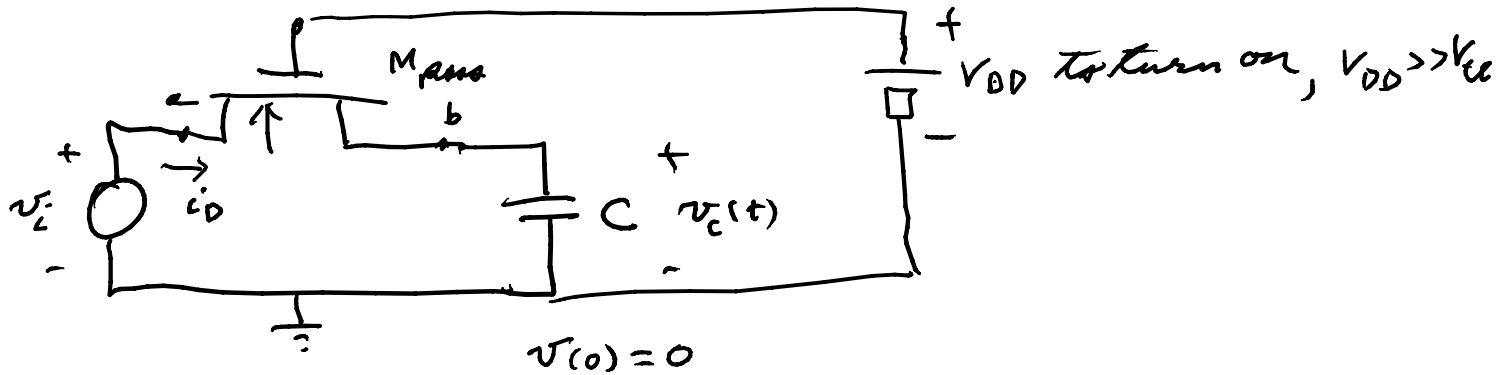


P. 236 $\epsilon_{\text{SiO}_2} = \epsilon_r \cdot \epsilon_0 = 3.9 \epsilon_0 = 3.45 \times 10^{-11} \text{ Fd/m}$

if $t_{\text{ox}} = 4 \text{ nm} \Rightarrow C_{\text{ox}} = 8.6 \times 10^{-3} \text{ Fd/m}^2$

if $W=L = 10 \mu\text{m} \Rightarrow A_{\text{gate}} = (10 \times 10^{-6})^2 = 10^2 \times 10^{-12} = 10^{-10} \text{ m}^2$

$C = 8.6 \times 10^{-3} \times 10^{-10} = 8.6 \times 10^{-13} = 86 \text{ fF}$
MOS transistor



$v_c(t) = V_{DD} 1(t)$

at $t=0$, $a=D$, $b=S$; $v_{GS} = V_{DD} - v_c = V_{DD} - 0$

$1(t) = \text{unit step}$

$v_{DS} = V_{DD} - 0 \leftarrow @ t=0$



if $a=D$, $b=S$

$v_{GS} = V_{DD} - v_c$

$v_{DS} = V_{DD} - v_c \Rightarrow v_{DS} > v_{GS} - V_{th}$

$\Rightarrow M_{\text{pmos}}$ is in saturation

$i_D = \beta (v_{GS} - V_{th})^2 = \beta (V_{DD} - v_c - V_{th})^2 = C \frac{dv_c}{dt} = C \frac{d(v_c - V_{DD} + V_{th})}{dt}$

let $x = v_c - V_{DD} + V_{th} \Rightarrow \beta x^2 = C \frac{dx}{dt}$, $x(0) = -V_{DD} + V_{th}$

$\beta = \frac{K_P W}{2L}$

a Riccati ODE

$\frac{\beta}{C} dt = \frac{dx}{x^2} \Rightarrow \int_0^t \frac{\beta}{C} dt = \int_{x(0)}^{x(t)} \frac{dx}{x^2}$

$\frac{\beta}{C} \cdot t = -\frac{1}{x} \Big|_{x(0)}^{x(t)} = -\frac{1}{x(t)} + \frac{1}{x(0)} \Rightarrow \frac{1}{x(t)} = \frac{1}{x(0)} - \frac{\beta}{C} t$

$$x(t) = \frac{1}{\frac{1}{x(0)} - \frac{\beta}{C}t} = \frac{x_0}{1 - \frac{\beta}{C}t}$$

$$i_s = x(0) = x_0 \text{ at } t=0$$

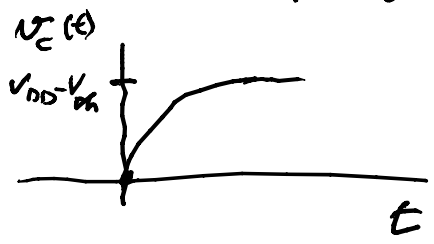


$t_0 = C/\beta = \text{finite escape time}$

$$v_c(t) = x(t) + V_{DD} - V_{th}$$

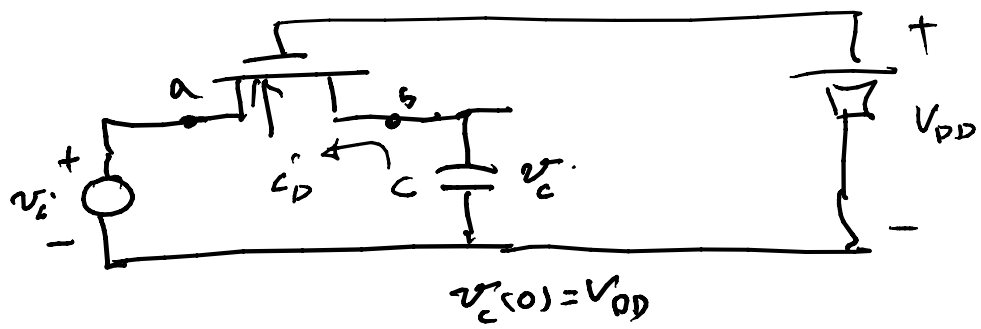
$$= \frac{-V_{DD} + V_{th}}{1 - \frac{\beta}{C}t} + V_{DD} - V_{th}$$

$$\text{as } t \rightarrow \infty \Rightarrow V_{DD} - V_{th}$$



note has a V_{th} loss

Look at passing from C to a short v_i



$$v_c(0) = V_{DD}$$

$$v_i(t) = 0$$

here $a=S, b=D \Rightarrow v_{GS} = V_{DD}, v_{DS} = v_c \leq V_{DD}$

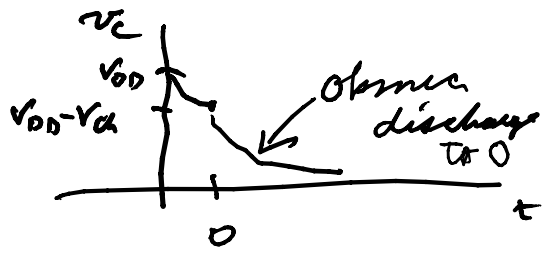
for a small time starts in sat.

$$v_{GS} - V_{th} = V_{DD} - V_{th} < v_c \text{ at } v_c(0) = V_{DD}$$

after $v_c \leq V_{DD} - V_{th}$ then

$$v_{GS} - V_{th} = V_{DD} - V_{th} \geq v_c$$

changes to ohmic region



$$-C \frac{dv_c}{dt} = i_D = \beta (2(V_{DD} - V_{th})v_c - v_c^2) = \beta (2(V_{DD} - V_{th}) - v_c)v_c$$

a new Riccati eq.

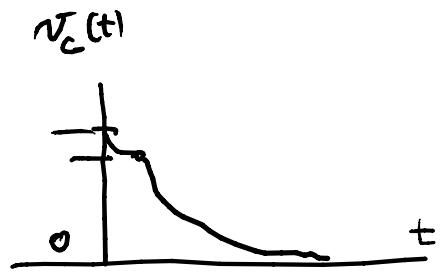
$$-\frac{\beta}{C} dt = \frac{dx}{(2(V_{DD} - V_{th}) - v_c)v_c} = \frac{dx}{(a-x)x} \quad \begin{matrix} a = 2(V_{DD} - V_{th}) \\ x = v_c \end{matrix}$$

$$= dx \left[\frac{k_0}{x} + \frac{k_1}{x-a} \right] \text{ via partial fraction expansion}$$

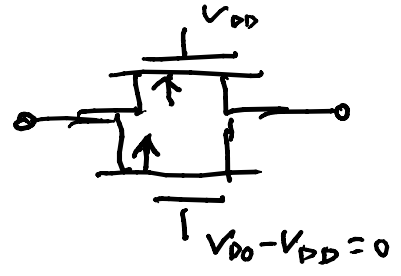
$$k_0 = \frac{\kappa}{(a-x)\kappa} \Big|_{x=0} = \frac{1}{a}, \quad k_a = \frac{(\kappa-a)}{(a-x)\kappa} \Big|_{x=a} = -\frac{1}{a}$$

$$-\frac{\beta}{c} t = \int_{x_0}^{x(t)} \frac{dy}{a} \left[\frac{1}{y} + \frac{-1}{y-a} \right] = \frac{1}{a} \left[\ln y - \ln(y-a) \right] \Big|_{x_0}^{x(t)}$$

$$= a \ln \frac{y}{y-a} \Big|_{x_0}^{x(t)} \quad \text{as } t \rightarrow \infty, \ln(1) \rightarrow 0$$

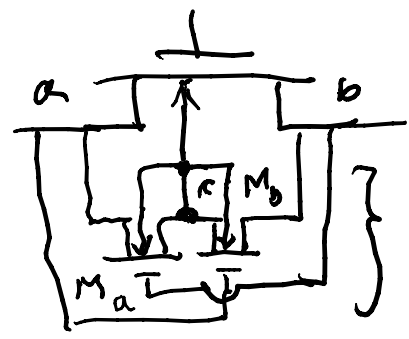


∴ to pass all the way in both directions



here if tie Bulk to one side then passes bulk current when that side is the drain

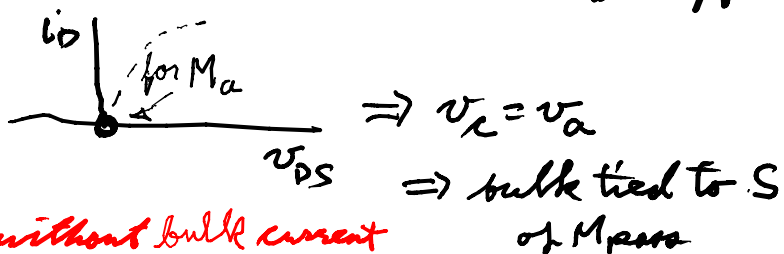
Look for a bulk bias circuit to tie the bulk to the source. Put on something like an inverter



bulk bias circuit

if $V_b > V_c \geq V_a$
then M_b is off
as $V_{GS} < V_{th}$

M_a is fully on but with no drain current (as M_b is off)



same result of $V_c = V_b$ if
if $V_b < V_a$

∴ can pass without bulk current

