

ENEE 303H Spring 2009 Final Exam

Open book, open notes. Your signature is required and certifies that the work is solely your own. 150 points total. If stuck be sure to go on to the next problem. Good Luck.

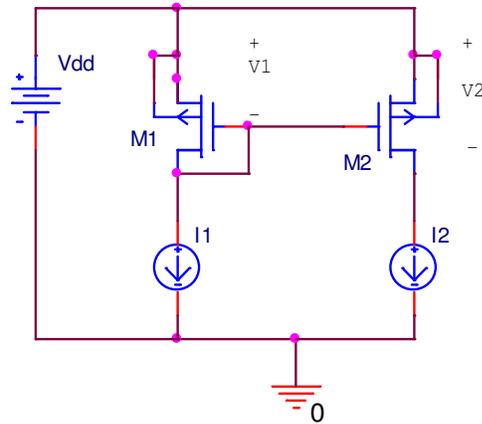
Use the following for transistor model Spice parameters:

For BJTs:  $\beta = 99$ ,  $V_T = 0.026V$  = thermal voltage,  $|V_{BE}| = 0.7V$

For CMOS:transistors:  $V_{TOn} = -V_{TOp} = 0.5 V$ ,  $C_{gs} = 20 pFd$ ,  $C_{gd} = 0$

$K_{Pn} = K_{Pp} = 10^{-5} A/V^2$ ;  $\lambda_n = \lambda_p = 0.02$

1. (50 pts, 30 min)

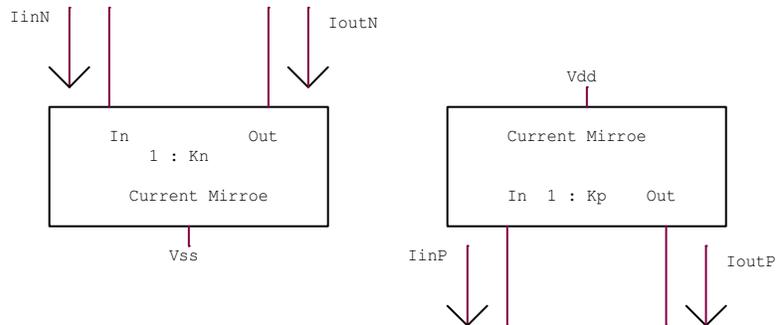


For the above circuit  $M1 = M2$  and  $V_{dd}$  is assumed as large as needed.

It is desired to have positive  $V2 = 2V1$ .

- Show that  $M2$  is in saturation.
- Find  $I2/I1$  as a function of  $V1$ .
- It is desired to design for  $V2 = 4$ ; find  $I1$  and  $I2$  when  $(W/L) = 2$ .

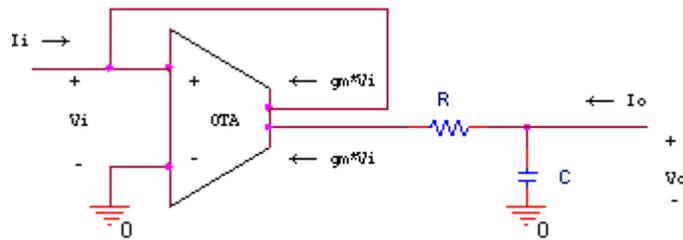
2. (40 pts, 25 min).



The above symbols represent two types of current mirrors for which DC currents can only flow in one direction.  $K_n$  and  $K_p$  are positive current gains. Assume that  $V_{dd} = -V_{ss} = 5V$  and the input transistors have  $(W/L) = 2$ .

- Draw a connection of the two types so that the overall current in and current out can flow in two directions to form a bidirectional current mirror.
- Draw an MOS transistor version of your bidirectional current mirror.
- Calculate  $I_{inN} = I_{inP}$  when the input current and voltage (wrt ground) are zero, .
- Discuss what happens when the current gains  $K_n$  and  $K_p$  differ.

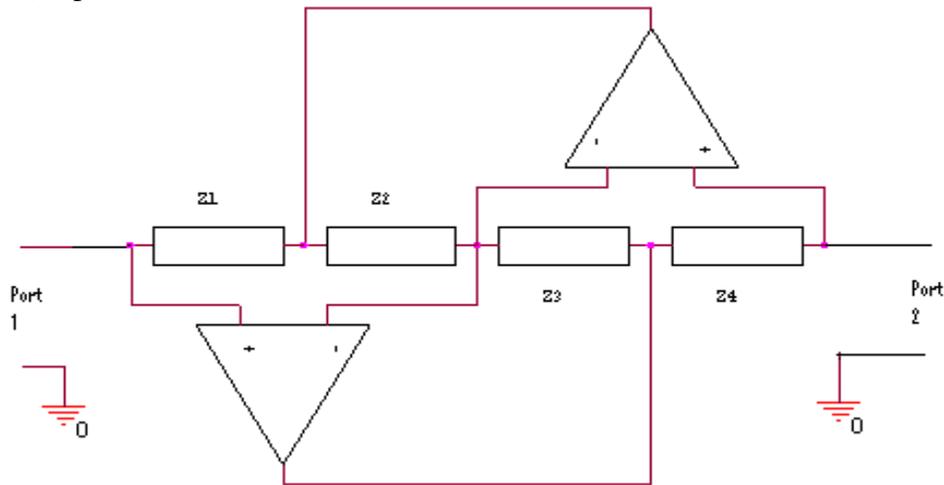
3. (40 pts, 25 min)



For this circuit assume the two output currents,  $I_{ota}$ , of the OTA are identical.

- If the OTA is described by  $I_{ota} = \alpha I_T \tanh(V_i / (2V_T))$  give  $gm$  when biased at  $V_i = 0$  [where  $I_{ota}$  is directed as the OTA output currents shown;  $I_T$  is the tail current].
- Find the 2-port admittance matrix  $Y(s)$  [valid for small signal  $v_i$ ] (in terms of  $gm$ ,  $R$ ,  $C$ ). Here port 1 is the input one (on the left) and port 2 is the output one (on the right).
- If a small step function of voltage  $v_i$  is applied,  $v_i(t) = V_i 1(t)$ , [1(.) = unit step function] and the output is open circuited,  $I_o = 0$ , give the differential equation for  $v_o(t)$  and solve assuming positive  $R$ ,  $C$ ,  $gm$  [assume  $v_o(t) = 0$  for  $t < 0$ ]

4. (20 points, 10 min)



- Draw a cascade connection of two identical copies of this circuit. [that is, port 2 of the first circuit directly connects to port 1 of the second with port 1 of the first and port 2 of the second being the new 2-port ports].
- Give a 2-port description of this cascade.
- If  $Z_1$  and  $Z_3$  are for capacitors and  $Z_2$  &  $Z_4$  are for resistors find the current gain of the cascade and discuss possible uses of the cascade.