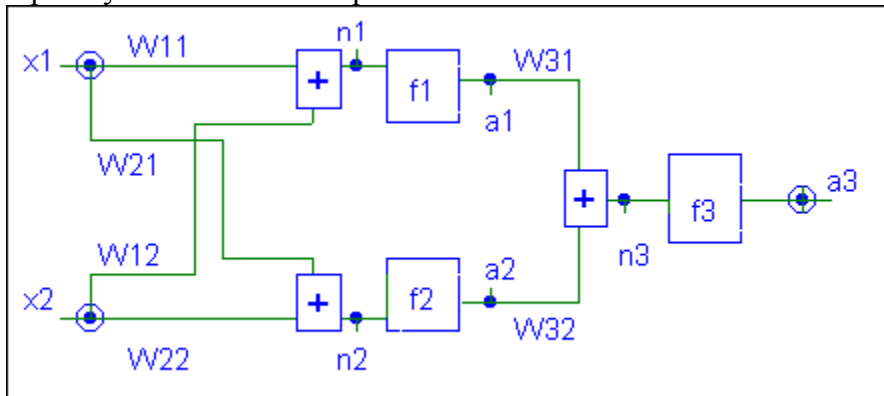


ENEE 434 Final Exam- Take Home Portion

Open book open notes; this portion is due at the beginning of the final period with penalties of a point per 5 minute late period.

1tkhm (100 points, 50 minutes)

A neural network has the structure shown, that is, it has two inputs,  $x_1$  and  $x_2$ , with four weights to two input layer neurons of activation functions,  $f_1$  &  $f_2$ , and one output layer neuron with a purelin activation function,  $f_3$ , with two weights to it from the input layer and overall output  $a_3$



- Give the expression for the output  $a_3$  as a function of the inputs, weights, and activation functions of the network.
- What restriction does the absence of biases place upon the class of functions  $a_3=y(x_1,x_2)$  which can be realized with no error?
- Assume that over the two dimensional square  $[0,1] \times [0,1]$  it is desired that this network approximate

$$y = \frac{1}{3}(x_1)^3 + (x_1)(x_2)$$

- Calculate the output error,  $y-a_3$ , for all weights being 1 and at  $x=[1, \frac{1}{2}]^T$  with  $f_1(z)=f_2(z)=\tanh(z)$  [recall that  $f_3$  is purelin].
- Give the sensitivity matrices of interest for backpropagation with the same conditions as in c1).
- Under the same conditions as c1) give the weight updates  $\Delta W_{ij}$  for the next update step.
- What is the error  $y-a_3$  after the update of c3)?