

ENEE 610 Fall 2019 Homework 5 Due Tu 10/08/19

#1 (50 points: lossless synthesis)

For the impedance $z(s) = [6s^3 + 4s] / [12s^4 + 14s^2 + 1]$

- a) Give the poles and zeroes and plot them in the s-plane.
- b) Give the four canonical circuits of Foster and Cauer.
- c) Repeat b) for the same function being an admittance $y(s)$, that is $y(s) = [6s^3 + 4s] / [12s^4 + 14s^2 + 1]$
- c) If a circuit for $z(s)$ is in parallel with a 1 Ohm resistor, give the new (parallel) impedance $z_p(s)$ and discuss its relation to an Hurwitz polynomial.

#2 (50 points, negative impedance converters).

- a) A 2-port has $i_2 = K_I i_1$ and $v_2 = K_V v_1$ where K_I and K_V are non-zero current and voltage gain constants of the same sign. Load the 2-port in an impedance $Z_L(s)$ and give (the negative impedance converted) $Z_{in}(s)$.
- b) Another form of negative impedance converter is shown in the following figure where R is a positive number (so the middle resistor is active). Find its 2-port impedance matrix, its 2-port scattering matrix and its Z_{in} when loaded in Z_L .
- c) When loading the following 2-port in Z_L and R is normalized to 1 Ohm (or $K_I = K_V$) find the scattering matrix (a reflection coefficient as $n=1$) for Z_{in} and compare with that of Z_L .

