

610 Fall 2018 – Homework 7 Due ~~Th 11/15/18~~ => Tu 11/20/18

1. (40 points,  $v_2/v_1$  ladder synthesis)
  - a. Synthesize the following as a lossless ladder 2-port loaded in a 1Ohm resistor and evaluate k
    - a)  $v_2/v_1 = k/[s^4 + 3s^3 + 8s^2 + 9s + 12]$
    - b)  $v_2/v_1 = ks^4/[s^4 + 3s^3 + 8s^2 + 9s + 12]$
    - c)  $v_2/v_1 = ks^2/[s^4 + 3s^3 + 8s^2 + 9s + 12]$
  - d) For each of the above cases give the 2-port admittance matrix,  $Y(s)$ . Check that  $Y(s)$  is lossless and compare.
  
2. (40 points, state variable synthesis)
  - a) Synthesize the lossless impedance  $z(s) = 3s(s^2+4)/(s^2+2)$  using a state space realization of its admittance  $y(s)$ . Comment about the pole of  $y$  at infinity.
  - b) Using a state space realization synthesize the all-pass function  $v_2/v_1 = [s^2 - as + b]/[s^2 + as + b]$  where  $a$  and  $b$  are any positive real parameters.
  
3. (20 points, all-pass Constant R)
  - a) Show that the Richards' section with admittance  $Cs$  replaced by  $y(s)$  is constant- $R$  and determine the lossless  $y(s)$  to give the all-pass function of problem 2.b) above.
  - b) Discuss how Richards' sections can be used to synthesize any rational all-pass  $v_2/v_1(s)$ .