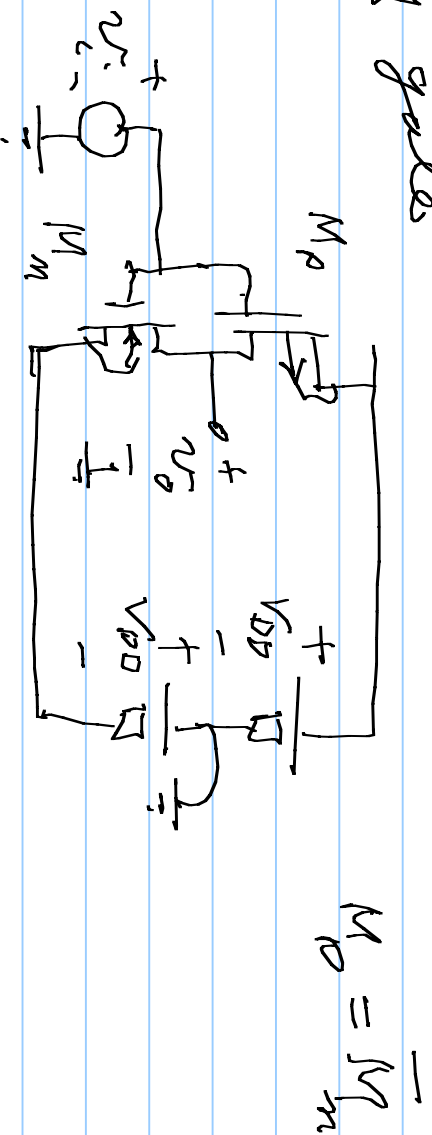


Midterm Th open book

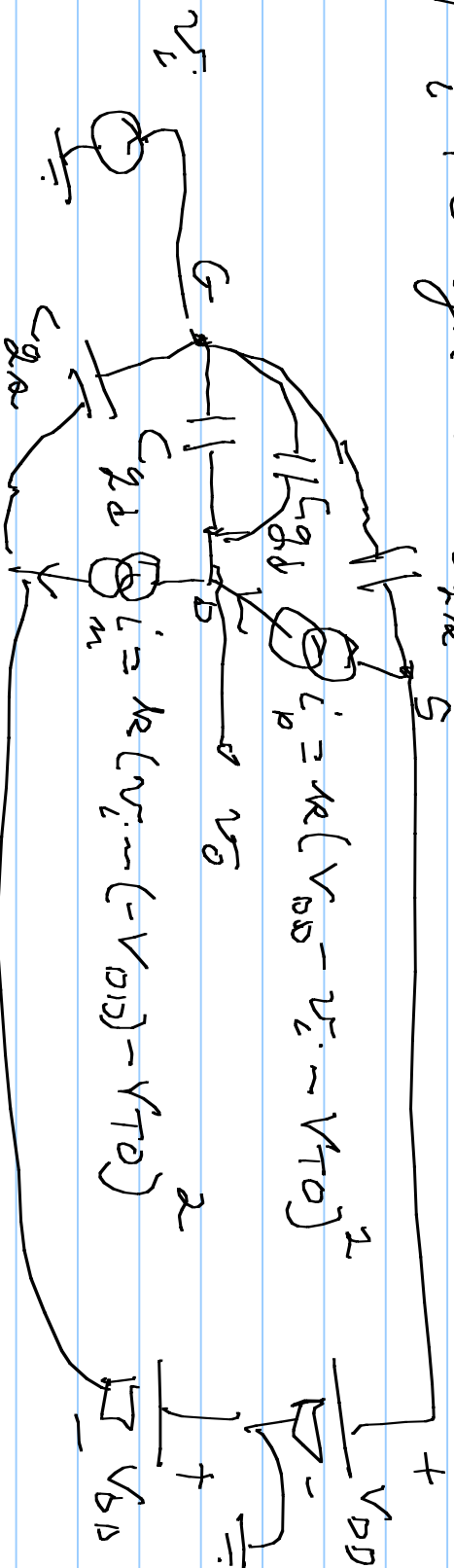
ternary gates



assume @ $t \leq 0^-$, $v_i = 0$, $v_o = 0$

if M_n & M_p are enhancement mode, $V_{DD} > 0$
 $\Rightarrow M_n$ & M_p are in saturation at $t > 0$

if $v_i \neq 0$ for $t > 0$ C_{gs}



$$\begin{aligned}
 i'_{C_{gs}} &= 2C_{gs} A(v_{i0} - v_i) = i_p - i_n \\
 &= k_p (V_{DD} - V_{T0})^2 - 2(V_{DD} - V_{T0})v_i + \underbrace{v_i^2}_{\leftarrow} \\
 &\quad - k_n (V_{DD} - V_{T0})^2 + 2(V_{DD} - V_{T0})v_i + v_i^3 \\
 &= k_p \left[-2(V_{DD} - V_{T0})v_i - 2(V_{DD} - V_{T0})v_i^2 \right] \\
 &= -4k_p (V_{DD} - V_{T0})v_i
 \end{aligned}$$

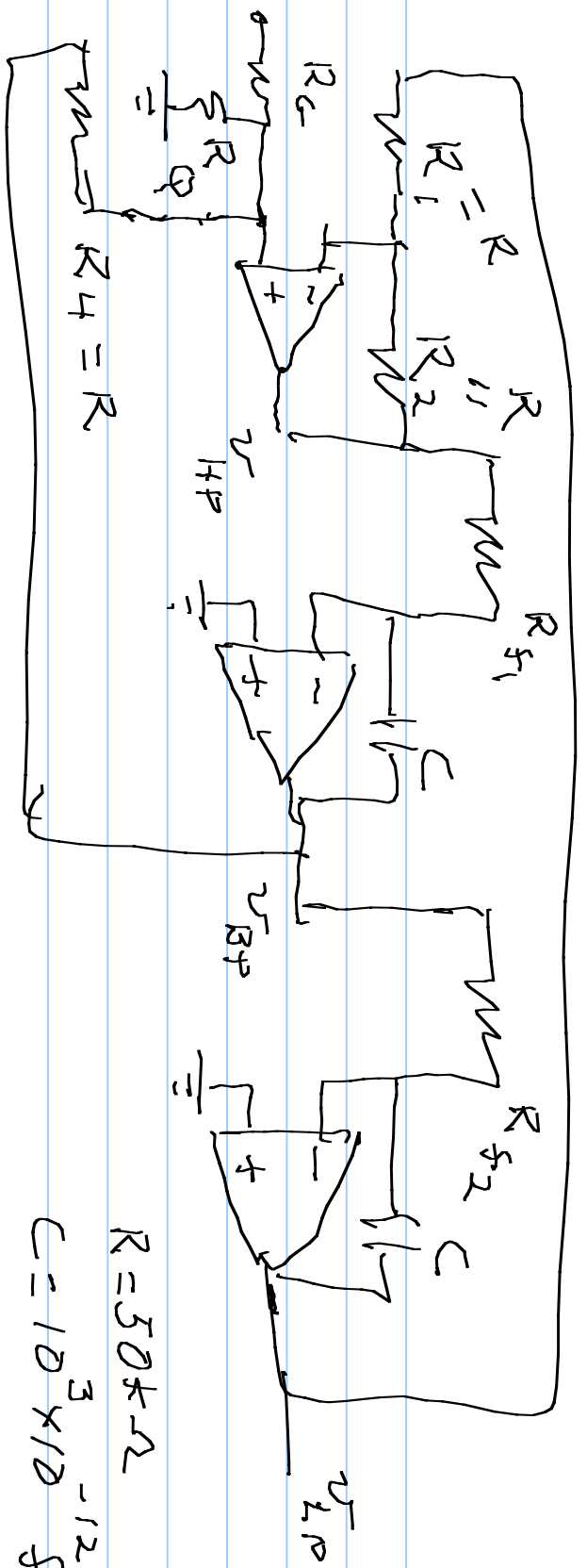
$$2C_{gd} \frac{dv_{gs}}{dt} = 2C_{gd} \frac{dv_{gs}}{dt} - 4k(V_{DD} - V_{T0})v_i$$

TF VAF = 4R

$$\text{Thus Pass } \frac{V_o(s)}{V_i} = \frac{A_{HP} \omega_m^2}{s^2 + \omega_n s + \frac{\omega_n^2}{Q}}$$

Design for noninverting pole - pass low pass

$$\omega_n = 5 \times 10^3, \quad Q = 50$$



$$A_{LP} = \frac{2}{R_G \left(\frac{1}{R_G} + \frac{1}{R_Q} + \frac{1}{R_U} \right)} = \frac{2/R_G}{\frac{1}{R_U} + \frac{1}{R_U}} = \frac{2R_U R_U \cdot 1}{R_U + R_U} R_G$$

$$\omega_n^2 = \frac{1}{R_{S1} R_{S2} C^2} = 5^2 \times 10^6 = 25 \times 10^6 = \frac{1}{R_{S1} R_{S2} \times 10^6 \times 10^{-24}}$$

$$\Rightarrow R_{S1} R_{S2} = \frac{10^{12}}{25} = 4 \times 10^{10}$$

$$Q = \frac{1 + R_4/R_{11}}{2} \left[\frac{R_{S1}}{R_{S2}} \right]^{1/2} = 50$$

$$R_{11} = \frac{R_G R_Q}{R_G + R_Q}$$

$$\frac{R_{S1}}{R_{S2}} = \frac{25 \times 10^2 \times 4}{\left(1 + (R_4/R_{11})\right)^2} = \frac{10^4}{\left(1 + (R_4/R_{11})\right)^2}$$

$$A_{LP} = 2 \frac{R_4}{R_G} \cdot \frac{1}{\left(1 + R_4/R_{11}\right)} ; \text{ choose } R_4 = R_G$$

$$= \frac{2}{1 + R_4/R_{11}}$$

$$R_{S1} = \frac{1}{R_{S2}} \times 4 \times 10^{10}$$

$$\frac{1}{2} \times 4 \times 10^{10} = \frac{10^4}{\left(1 + \frac{R_4}{R_{11}}\right)^2}$$

$$R_{S2}^2 = \frac{4 \times 10^{10}}{10^4} \times \left(1 + \frac{R_4}{R_{11}}\right)^2$$

$$R_{S2} = 2 \times 10^3 \left(1 + \frac{R_4}{R_{11}} \right)$$

$$= 2 \times 10^3 (1 + 2)$$

$$= 4 \text{ k}\Omega$$

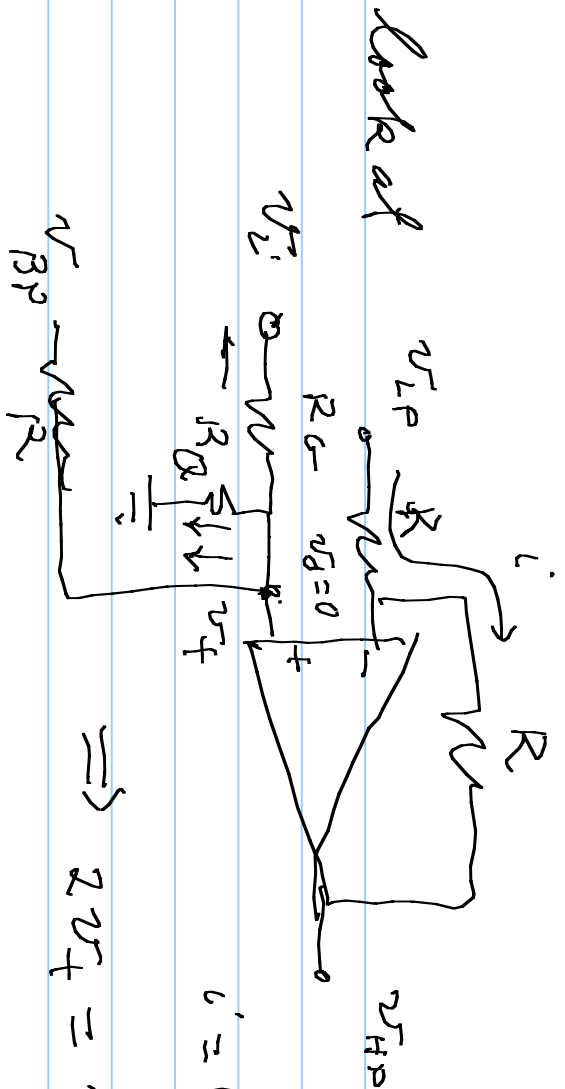
$$\text{if } R_{11} = \frac{R_G R_Q}{R_G + R_Q} = \frac{1}{2} R$$

$$\Rightarrow R_G = R_Q$$

$$R_{S1} = \frac{4}{4 \times 10^3} \times 10^6 = 1 \times 10^3 = 1 \text{ k}\Omega$$

$A_{LP} = \frac{2}{1+2} = 2/3$ gain @ DC for all resistors equal

$$\frac{V_O}{V_i} = \frac{\frac{2}{3} \times (5 \times 10^3)^2}{2^2 + \frac{5 \times 10^3}{50} \times 2 + (5 \times 10^3)^2}$$



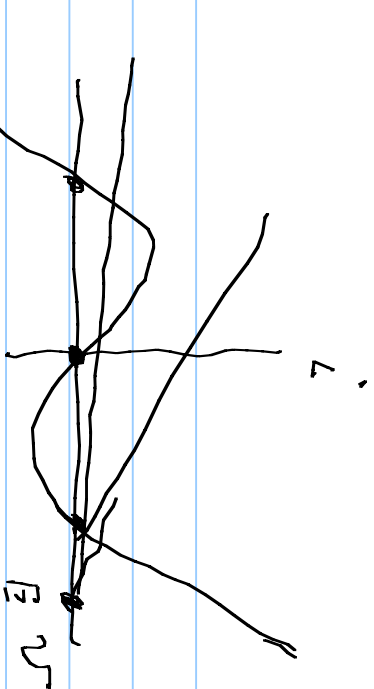
$$i' = (v_{LP} - v_f) G = G(v_f - v_{HP})$$

$$\Rightarrow 2v_f = v_{LP} + v_{HP}$$

$$(v_f - v_{LP}) G_G + v_f G_Q + (v_f - v_{BP}) G = 0$$

solve for $v_f \Rightarrow \frac{v_{LP} + v_{HP}}{2}$ gives v_f in terms of v_{LP}, v_{HP}, v_{BP}

small signal diode



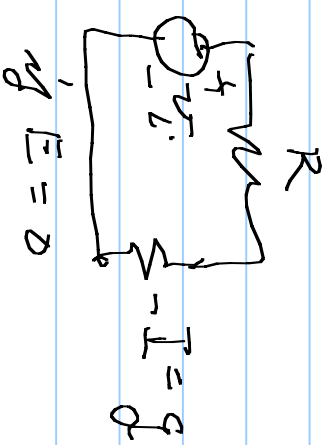
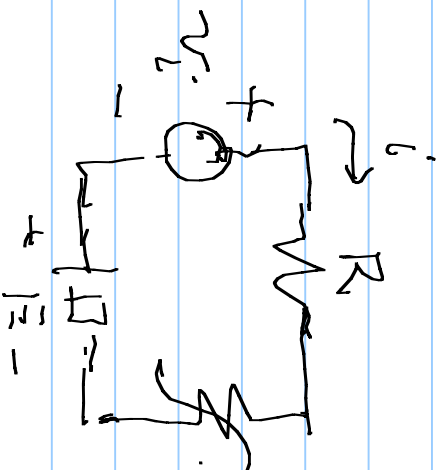
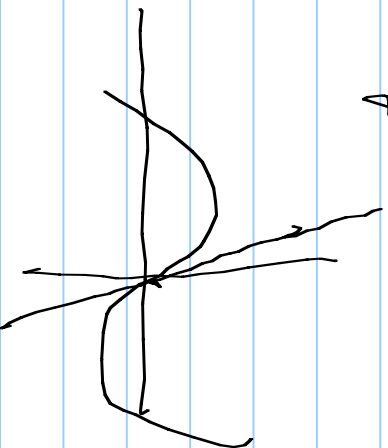
$$i = I(n-1), n(n+1)$$

$$g @ v = 0$$

$$g = \frac{di}{dv} = I \{ 2n(n+1) + (n-1)(n+1) + (n-1)2n \}$$

$$i |_{v=0} = 0$$

$$g |_{v=0} = -I$$



$$i = v_i \left[\frac{1}{R} - \frac{1}{I} \right]$$

\Rightarrow Can give power if $R < \frac{I}{I}$ then the current flows into the source

