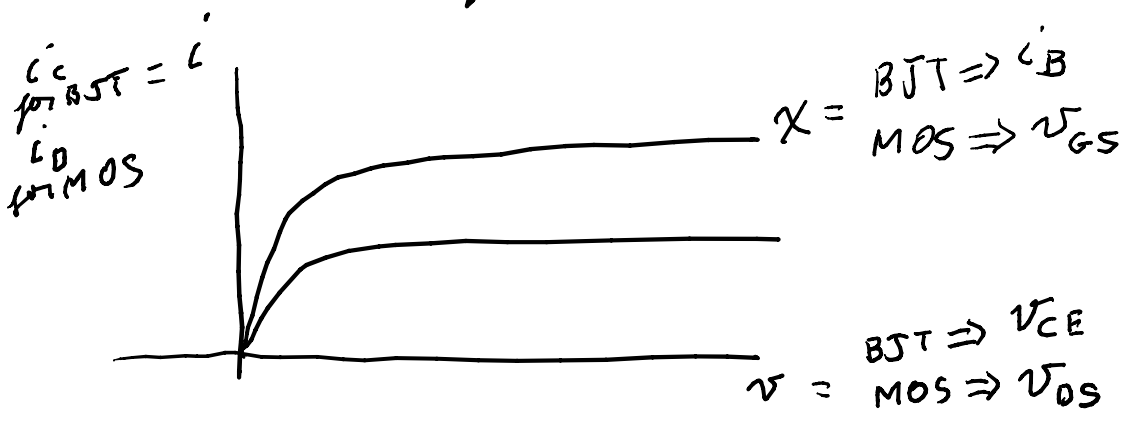
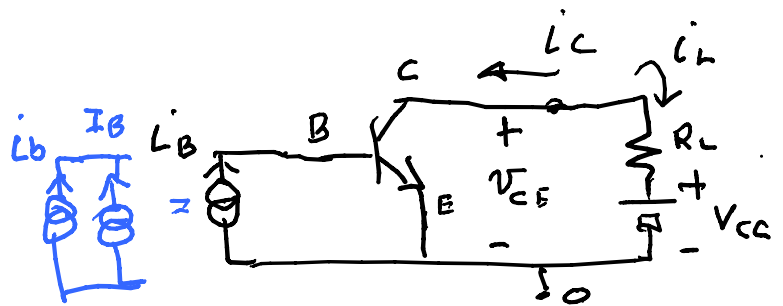


to get pnp requires another diffusion



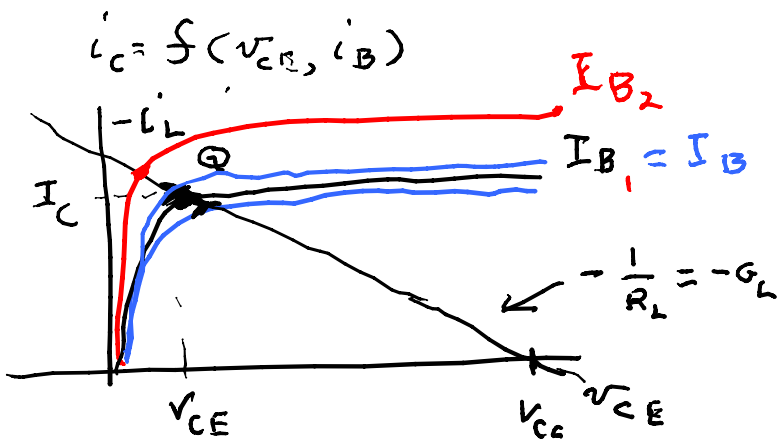
$$i = f(v, x)$$



$$v_{CE} = R_L i_L + V_{CC}$$

$$i_C = -i_L \downarrow$$

$$i_L = \frac{1}{R_L} (v_{CE} - V_{CC}) \Rightarrow -i_L = \frac{1}{R_L} (V_{CC} - v_{CE})$$



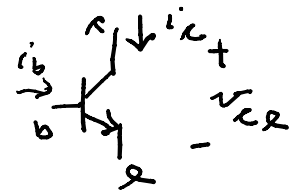
$i_B = \text{total} = I_B + i_b$ usually assume $|i_b| \text{ small} \ll I_B$

$I_B = \text{bias}$

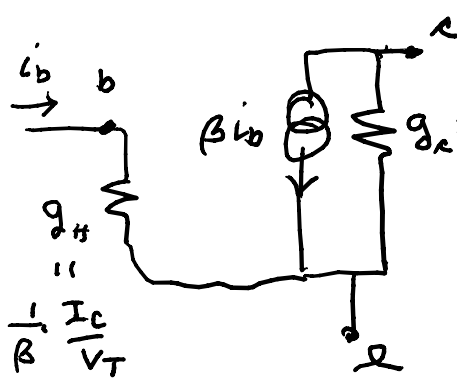
$i_b = \text{signal}$

$$i_C = f(v_{CE}, i_B) = \underbrace{f(v_{CE}, I_B)}_{I_C} + \frac{\partial f}{\partial v_{CE}} \Big|_Q (v_{CE} - V_{CE}) + \frac{\partial f}{\partial i_B} \Big|_Q (i_b - I_B) + \dots$$

$$i_c - I_C = i_c \approx \left. \frac{\partial i_c}{\partial v_{CE}} \right|_Q \cdot v_{ce} + \left. \frac{\partial i_c}{\partial i_B} \right|_Q \cdot i_b$$

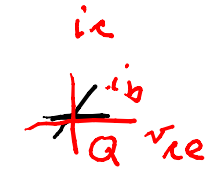


$$i_c = g_m \cdot v_{ce} + \beta \cdot i_b$$

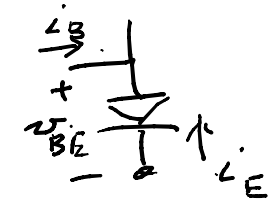


$$g_m = \frac{I_C}{V_A} = \frac{\Delta i_c}{\Delta v_{CE}} \Big|_Q$$

small signal equivalent circuit



The BJT is forward biased here.



$$-i_E = I_S (e^{v_{BE}/V_T} - 1)$$

$$\left. \frac{\partial i_E}{\partial v_{BE}} \right|_Q = \frac{I_S}{V_T} \cdot e^{v_{BE}/V_T} \approx \frac{I_S (e^{v_{BE}/V_T} - 1)}{V_T} \Big|_Q = \frac{-I_E}{V_T} = -g_{be} = -g_d$$

$$i_c = \beta i_B = -\alpha i_E \Rightarrow i_B = -\frac{\alpha}{\beta} i_E \Rightarrow i_b = -\frac{\alpha}{\beta} (-g_d) v_{be} = g_{\pi} v_{be}$$

$$i_b = -\frac{\alpha}{\beta} i_c$$

$$\frac{\alpha}{\beta} = \frac{\alpha}{1-\alpha} = 1-\alpha$$

$$g_{\pi} = \frac{\beta}{\beta+1} \times \frac{1}{\beta} \cdot (g_d) = \frac{-I_E}{V_T} \cdot \frac{1}{\beta+1}$$

$$\beta = \frac{\alpha}{1-\alpha} \Rightarrow \beta - \alpha\beta = \alpha$$

$$\Rightarrow \beta = \alpha(\beta+1)$$

but $I_C = -\alpha I_E$

$$= \frac{\alpha}{\beta} \cdot \frac{I_E}{V_T} = \frac{I_C}{\beta V_T}$$

$$I_E = -\frac{1}{\alpha} I_C$$

$$\Rightarrow \alpha = \beta/\beta+1$$

$$g_{\pi} = \frac{I_C}{\beta V_T}$$