

610 Fall 2012 – Homework 2

1. For the circuit giving the semistate equations covered in the class notes of 09/06/12 replace the VCCS by an ideal op-amp (necessitating adding a branch 7 across C1); also add a resistor R1 in series with v_i as part of branch 1.

- a) Give the new graph, the new cut-set and tie-set matrices, and the $Av=Bi$ descriptions using as much of the graph used in class as possible.
- b) From those give the semistate equations using v_t and i_l as components of the semistate x .
- c) Indicate what problems are anticipated in using these equations if $R1=0$.

2. A circuit has the following semistate matrices:

$$E := \begin{pmatrix} 0 & 0 & 0 & 0 \\ C1 & 0 & 0 & 0 \\ 0 & 0 & 0 & L1 \\ 0 & 0 & 0 & 0 \end{pmatrix} \quad \underline{A} := \begin{pmatrix} 0 & g1 & 0 & 0 \\ -g1 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \\ g1 & 0 & -1 & 0 \end{pmatrix} \quad B := \begin{pmatrix} 0 & 1 \\ 0 & 1 \\ 1 & 0 \\ 1 & 0 \end{pmatrix} \quad \underline{C} := \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}$$

Assuming that C1, L1 and g1 are all positive

- a) transform the system so that E is the direct sum of I_2 and O_2 .
 - b) Eliminate the last two rows to obtain state variable equations.
 - b) Find the transfer function 2x2 matrix, $T(s)=C(sE-A)^{-1}B$, where E is the above 4x4 matrix.
3. Find the characteristic polynomial and the minimal polynomial for the 4x4 A matrix of problem 2 above.
4. Find a singular valued decomposition for the above E. for C1=2, L1=5. In MathCad this can be done with the following commands (after setting array origin to 1 in the tools, worksheet options, menu)

$$M := \text{svd2}(E) \quad M = \begin{pmatrix} \{4,1\} \\ \{4,4\} \\ \{4,4\} \end{pmatrix} \quad \underline{s} := M_1 \quad \text{sd} := \text{diag}(s) \quad U := M_2 \quad \underline{V} := M_3$$

Note that U and V are orthogonal matrices and check by

$$E2 := U \cdot \text{sd} \cdot V$$