

$$\frac{\beta}{C} \cdot t = \int_{x(0)}^{x(t)} \frac{-1/a}{x} dx + \int_{x(0)-a}^{x(t)-a} \frac{1/a}{x-a} dx$$

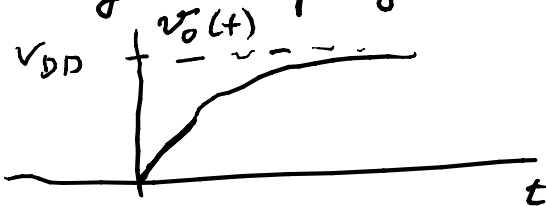
$$= -\frac{1}{a} \ln x \Big|_{x(0)}^{x(t)} + \frac{1}{a} \ln(x-a) \Big|_{x(0)}^{x(t)}$$

$$= \frac{1}{a} \left\{ -\ln\left(\frac{x(t)}{x(0)}\right) + \ln\left(\frac{x(t)-a}{x(0)-a}\right) \right\} = \frac{1}{a} \ln\left(\frac{x(t)-a}{x(0)-a} \times \frac{x(0)}{x(t)}\right)$$

$x = V_{DD} - v_o$   
 $a = 2(V_{DD} - |V_{T0}|)$   
 $\beta = \frac{K_P \cdot W}{2L}$  (PMOS)

$e^{\frac{a\beta}{C} t} = \left(\frac{x(t)-a}{x(0)-a}\right) \times \frac{x(0)}{x(t)}$  look @ home

here 0 is shifted from switching time of inverters input to time of change of PMOS from saturation to ohmic



Look at the latch p. 1205

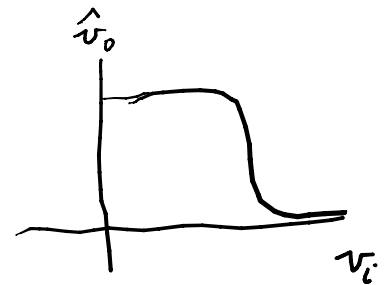
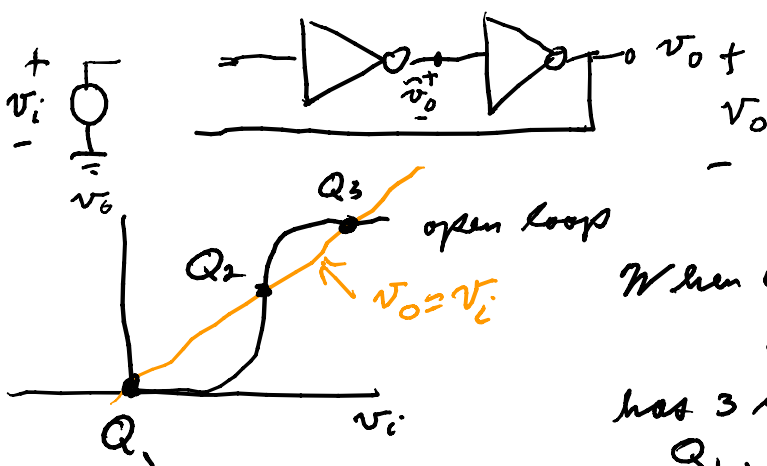
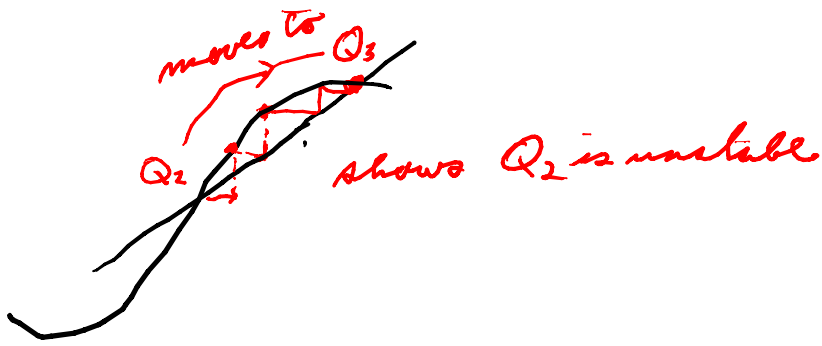


Fig 15.1

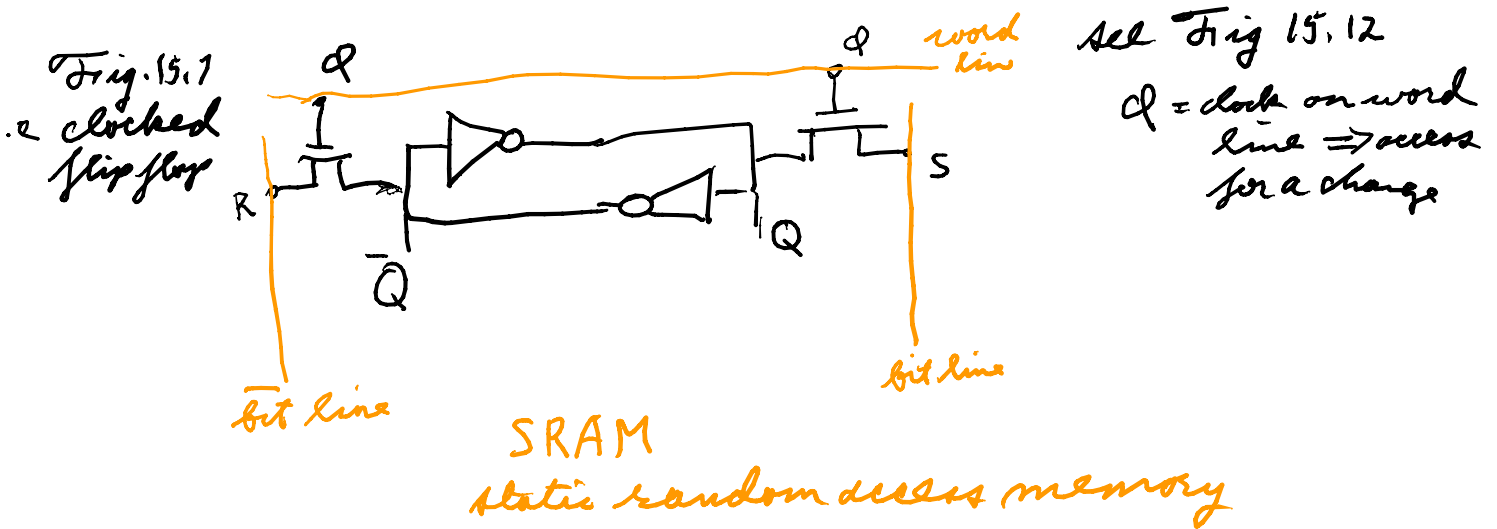
When does the feedback loop  
 $v_o = v_i$   
 has 3 rest points  
 $Q_1, Q_2, Q_3$   
 ↑ unstable  
 stable



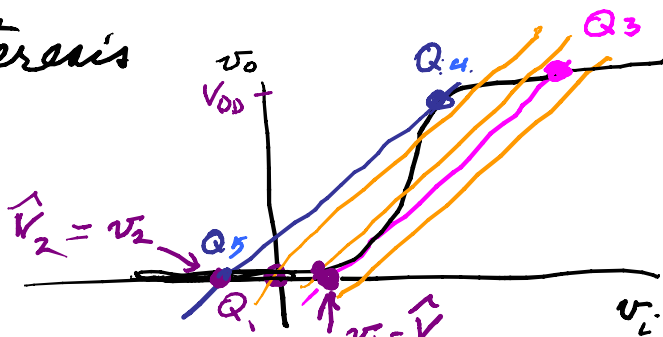
This latches the output for any little input

To make flip-flops go to Fig. 15.3

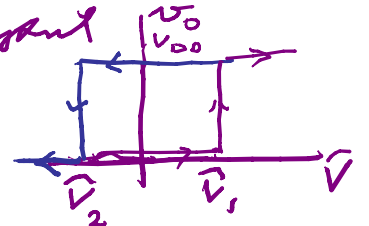
But first look at memory using the latch  
use a stable equilibrium point to remember



Hysteresis



let  $\hat{V}$  be a parameter if it is the actual input

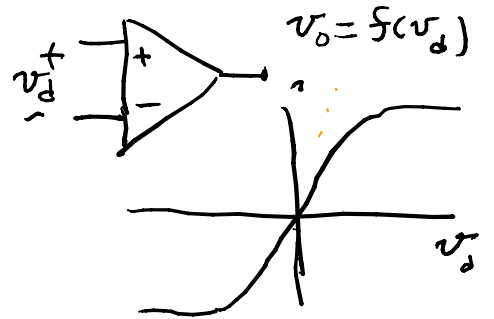
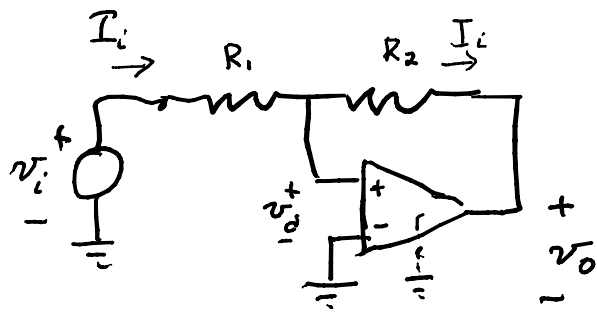


if start at  $Q_1$  we have to jump to  $Q_3$  when move to violet line.

if start at  $Q_3$  and decrease until slopes are equal we jump at  $Q_4$  to  $Q_5$

gives hysteresis of width  $\hat{V}_1 - \hat{V}_2$ , see p. 1357

To make  $\rightarrow$  need positive feedback



$$I_i = (v_i - v_d) \cdot G_1 = (v_d - v_o) G_2$$

$$\frac{G_1}{G_2} (v_i - v_d) = v_d - v_o \Rightarrow v_o = v_d + \frac{G_1}{G_2} v_d - \frac{G_1}{G_2} v_i$$

have load line  
with slope  $(1 + \frac{G_1}{G_2})$  &

intersect of  $v_i = \frac{G_2}{G_1} (1 + \frac{G_1}{G_2}) v_d$

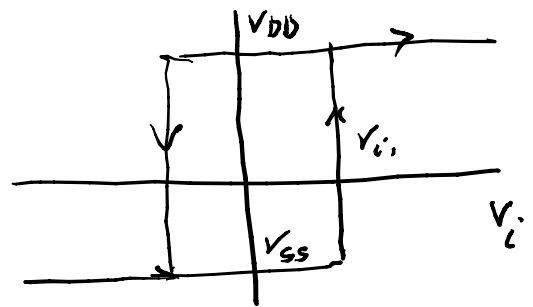
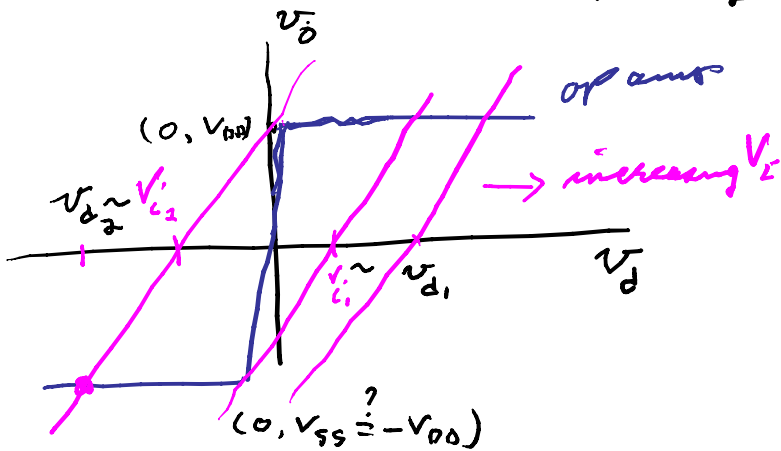
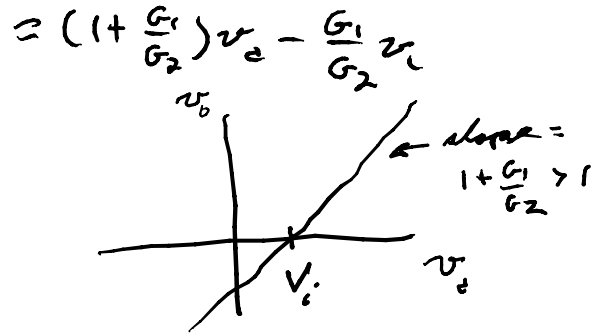


Fig 17.20

$$v_i \text{ is at } v_{d1} = \left[ \frac{G_1}{G_2} \left( 1 + \frac{G_1}{G_2} \right) \right] v_{i1}, \quad v_{d2} = \frac{G_1}{G_2} + \frac{1}{1 + \frac{G_1}{G_2}} v_{i2}$$

here  $\left( \frac{V_{DD}}{v_{d2}} \right) = \text{slope of right triangle}$