

Hw #1

ENEE610

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10/18/05

1) a)

$$\text{cutset matrix} = C = \begin{bmatrix} 1 & 0 & 0 & 0 & 1 & 1 & 1 & 1 \\ 0 & 1 & 0 & 0 & 1 & 1 & 0 & 1 \\ 0 & 0 & 1 & 0 & 1 & 0 & 0 & 1 \\ 0 & 0 & 0 & 1 & 0 & -1 & -1 & -1 \end{bmatrix}$$

Tieset Matrix = T =

$$\begin{bmatrix} -1 & -1 & -1 & 0 & 1 & 0 & 0 & 0 \\ -1 & -1 & 0 & 1 & 0 & 1 & 0 & 0 \\ -1 & 0 & 0 & 1 & 0 & 0 & 1 & 0 \\ -1 & -1 & -1 & 1 & 0 & 0 & 0 & 1 \end{bmatrix}$$

b)

$$C^T = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \\ 1 & 1 & 1 & 0 \\ 1 & 1 & 0 & -1 \\ 1 & 0 & 0 & -1 \\ 1 & 1 & 1 & -1 \end{bmatrix}$$

$$CC^T = \begin{bmatrix} 5 & 3 & 2 & -3 \\ 3 & 4 & 2 & -2 \\ 2 & 2 & 3 & -1 \\ -3 & -2 & -1 & 4 \end{bmatrix}$$

$$\Rightarrow \det(CC^T) = 45$$

HW #1  
c

ENEEG10

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$$A_a = \begin{bmatrix} 1 & 0 & 0 & 1 & 1 & 0 & 0 & 0 \\ -1 & 1 & 0 & 0 & 0 & 0 & -1 & 0 \\ 0 & -1 & 1 & 0 & 0 & -1 & 0 & 0 \\ 0 & 0 & 0 & -1 & 0 & 1 & 1 & 1 \\ 0 & 0 & -1 & 0 & -1 & 0 & 0 & -1 \end{bmatrix}$$

$$A = \begin{bmatrix} 1 & 0 & 0 & 1 & 1 & 0 & 0 & 0 \\ -1 & 1 & 0 & 0 & 0 & 0 & -1 & 0 \\ 0 & -1 & 1 & 0 & 0 & -1 & 0 & 0 \\ 0 & 0 & 0 & -1 & 0 & 1 & 1 & 1 \end{bmatrix}$$

d

$$A_a A_a^T = \begin{bmatrix} 3 & 1 & 0 & -1 & -1 \\ -1 & 3 & -1 & -1 & 0 \\ 0 & -1 & 3 & -1 & -1 \\ -1 & -1 & -1 & 4 & -1 \\ -1 & 0 & -1 & -1 & 3 \end{bmatrix}$$

$$\Rightarrow \det(A_a A_a^T) = 0$$

Since  $\det(A_a A_a^T) = \det(A_a) \det(A_a^T)$  and  $\det(A_a) = \det(A_a^T) =$

So  $\det(A_a A_a^T) = 0$  Also  $A_a A_a^T$  is symmetric

The result of problem 3.12 is incorrect since it says that the number of trees in a graph is equal to  $\det(A_a A_a^T)$

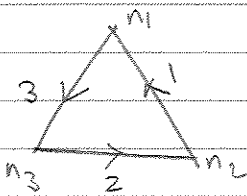
$$\textcircled{c} \det(AA^T) = \det \begin{bmatrix} 3 & -1 & 0 & -1 \\ -1 & 3 & -1 & -1 \\ 0 & -1 & 3 & -1 \\ -1 & -1 & -1 & 4 \end{bmatrix} = 45$$

So we conclude that  $\det(AA^T) = 45 = \det(CCT)$

So the correction to problem 3.12 would be this: The number of trees  $n_t$  is given by:  $n_t = \det(AA^T)$

in which  $A$  is the incident matrix of the graph which does not include the ground node in the graph.

Example:



Choose  $n_3$  as ground

number of trees = 3

$$A = \begin{bmatrix} -1 & 0 & 1 \\ 1 & -1 & 0 \end{bmatrix} \Rightarrow A^T = \begin{bmatrix} -1 & 1 \\ 0 & -1 \\ 1 & 0 \end{bmatrix}$$

$$\det(AA^T) = 3 = \text{number of trees}$$