

a) (10)

Tree branches: 3, 4, 5, 6

Cut set 1: (3, 1, 7)  $i_1+i_3+i_7=0$   
 Cut set 2: (4, 2, 7)  $i_2+i_4-i_7=0$   
 Cut set 3: (5, 1, 2, 7)  $i_1-i_2+i_5+i_7=0$   
 Cut set 4: (6, 1, 2, 7)  $-i_1+i_2+i_6-i_7=0$

Cut set Matrix:

$$C := \begin{bmatrix} 1 & 0 & 1 & 0 & 0 & 0 & 1 \\ 0 & 1 & 0 & 1 & 0 & 0 & -1 \\ 1 & -1 & 0 & 0 & 1 & 0 & 1 \\ -1 & 1 & 0 & 0 & 0 & 1 & -1 \end{bmatrix}$$

Tie set 1: (1, 3, 5, 6)  $V_1-V_3-V_5+V_6=0$   
 Tie set 2: (2, 4, 5, 6)  $V_2-V_4+V_5-V_6=0$   
 Tie set 3: (7, 3, 4, 5, 6)  $V_7-V_3+V_4-V_5+V_6=0$

Tie set Matrix:

$$T := \begin{bmatrix} 1 & 0 & -1 & 0 & -1 & 1 & 0 \\ 0 & 1 & 0 & -1 & 1 & -1 & 0 \\ 0 & 0 & -1 & 1 & -1 & 1 & 1 \end{bmatrix}$$

b) (5)

Admittance matrix:

$$Y_{bb} := \begin{bmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ gm & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & gm & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & G & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & G & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{bmatrix}$$

Using equality  $-C*j=C*Y_{bb}*C^T*V_t$

$$\text{Left} := -C*j$$

$$j := \begin{bmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ i \end{bmatrix}$$

$$\begin{bmatrix} 1 & 0 & 1 & 0 & 0 & 0 & 1 \\ 0 & 1 & 0 & 1 & 0 & 0 & -1 \\ 1 & -1 & 0 & 0 & 1 & 0 & 1 \\ -1 & 1 & 0 & 0 & 0 & 1 & -1 \end{bmatrix} \cdot \begin{bmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ i \end{bmatrix} = \begin{bmatrix} i \\ -i \\ i \\ -i \end{bmatrix} \quad \text{Left} := \begin{bmatrix} -i \\ i \\ -i \\ i \end{bmatrix}$$

Right =  $-C \cdot Y_{bb} \cdot C^T \cdot V_t$

Evaluate  $C \cdot Y_{bb} \cdot C^T$

$$\begin{bmatrix} 1 & 0 & 1 & 0 & 0 & 0 & 1 \\ 0 & 1 & 0 & 1 & 0 & 0 & -1 \\ 1 & -1 & 0 & 0 & 1 & 0 & 1 \\ -1 & 1 & 0 & 0 & 0 & 1 & -1 \end{bmatrix} \cdot \begin{bmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ gm & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & gm & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & G & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & G & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{bmatrix} \cdot \begin{bmatrix} 1 & 0 & 1 & -1 \\ 0 & 1 & -1 & 1 \\ 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \\ 1 & -1 & 1 & -1 \end{bmatrix}$$

$$C \cdot Y_{bb} \cdot C^T = \begin{bmatrix} gm & 0 & gm & -gm \\ 0 & gm & -gm & gm \\ 0 & 0 & G & 0 \\ 0 & 0 & 0 & G \end{bmatrix}$$

$$\begin{bmatrix} -i \\ i \\ -i \\ i \end{bmatrix} = \begin{bmatrix} gm & 0 & gm & -gm \\ 0 & gm & -gm & gm \\ 0 & 0 & G & 0 \\ 0 & 0 & 0 & G \end{bmatrix} \times \begin{bmatrix} V3 \\ V4 \\ V5 \\ V6 \end{bmatrix}$$

$$\begin{bmatrix} V3 \\ V4 \\ V5 \\ V6 \end{bmatrix} = \begin{bmatrix} \frac{1}{gm} & 0 & -\frac{1}{G} & \frac{1}{G} \\ 0 & \frac{1}{gm} & \frac{1}{G} & -\frac{1}{G} \\ 0 & 0 & \frac{1}{G} & 0 \\ 0 & 0 & 0 & \frac{1}{G} \end{bmatrix} \cdot \begin{bmatrix} -i \\ i \\ -i \\ i \end{bmatrix} = \begin{bmatrix} -\frac{1}{gm} \cdot i + \frac{2}{G} \cdot i \\ \frac{1}{gm} \cdot i - \frac{2}{G} \cdot i \\ -\frac{1}{G} \cdot i \\ \frac{1}{G} \cdot i \end{bmatrix}$$

$$\begin{bmatrix} V3 \\ V4 \\ V5 \\ V6 \end{bmatrix} := \begin{bmatrix} -\frac{1}{gm} \cdot i + \frac{2}{G} \cdot i \\ \frac{1}{gm} \cdot i - \frac{2}{G} \cdot i \\ -\frac{1}{G} \cdot i \\ \frac{1}{G} \cdot i \end{bmatrix}$$

$$V_{in} = -V_7 = -V_3 + V_4 - V_5 + V_6$$

$$V_{in} := 2 \cdot \left( \frac{1}{gm} - \frac{1}{G} \right) \cdot i$$

Input admittance:  $Y(s) = i/V_{in}$

$$Y(s) := \frac{1}{2 \cdot \left( \frac{1}{gm} - R \right)}$$

c) (5)

as the example, replacing C by L:

This time look for zeros and poles of  $(Z(s)+Ls)$ :

From note:09/15/04

$$Z(s) := 2 \cdot \frac{((1 - gm \cdot R) + s \cdot R \cdot (4 \cdot C_{gd} + C_{gs}))}{(gm + s \cdot C_{gs}) \cdot (1 + 4 \cdot s \cdot R \cdot C_{gs})}$$