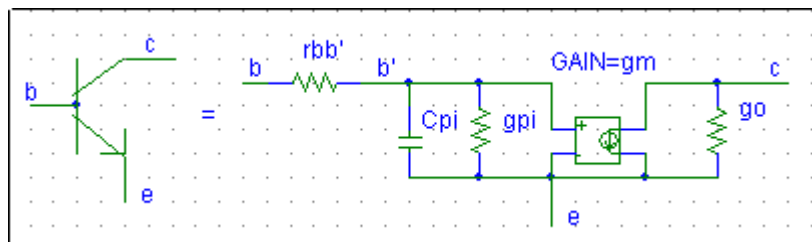


Some 2-Port Theory and State Equations

1. (35 points)

The following three-terminal 2-port, drawn using PSpice schematic components, is the standard hybrid-pi equivalent circuit for the BJT as shown (where the parameters are defined via the bias collector current I_c , thermal voltage $V_T = kT/q$ [$\approx 26\text{mV}$ at room T], transistor dc beta, and forward Early voltage V_A as $g_m = I_c/V_T = \text{transconductance}$, $g_o = I_c/V_A = \text{output conductance}$, $g_{pi} = g_m/\beta = \text{base-emitter diode conductance}$. Also $r_{bb'}$ is the base spreading resistance and C_{pi} the base-emitter diode capacitance)



- Find the admittance matrix $Y(s)$ using the symbols of the schematic. Use $v_1 = v_{be}$, $v_2 = v_{ce}$, $i_1 = i_b$, $i_2 = i_c$ as the port variables.
- For $I_c = 2\text{mA}$, $V_A = 100\text{V}$, $\beta = 50$, $r_{bb'} = 10\Omega$, and $C_{pi} = 20\text{pF}$, evaluate $Y(s)$ at room temperature.
- For the conditions of b) evaluate both the Hermitian part and the real part of $Y(s)$ in $\text{Re}(s) > 0$.
- Why is this transistor equivalent circuit not passive when a transistor is just a connection of inert material?

2. (35 points).

For the driving point impedance

$$z(s) = \frac{2s(s+2)}{(s+8)(s^2+25)}$$

- Give a set of state variable equations $dx/dt = Ax + Bu$, $y = Cx + Du$ with $u = i$, $y = v$.
- Draw a PSpice schematic for the state variable equations of a) using capacitors to give the derivatives and G components for the other terms.
- Run Spice when $u = 3\cos(5t)$ with $x(0) = 0$ and plot y for t between 0 and 2 seconds.