

## ENEE 610

## Homework Problems for Grading, Set 1 (60 points)

Due at class M 09/15/03

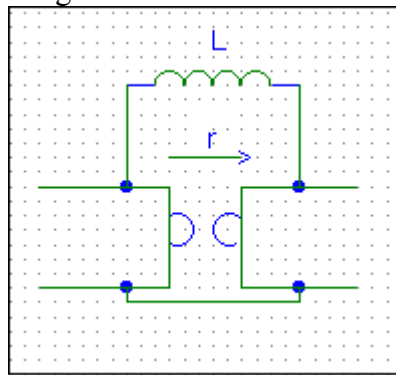
## Richards' Function Use and Some Theory

1. (30 points) For the following 2-port, when loaded on the right port by the impedance  $z_L$

a) find the input impedance  $z_{in}$  seen looking into the left port in terms of  $z_L$ ,  $r$  (gyration resistance), and  $L$ .

b) express  $z_L$  as one of the four Richards' functions of the "to consider, problem 2 of set 1 of 09/03/03,"

c) give the resulting values of  $L$  and  $r$  in terms of  $k$  and  $z_{in}(k)$



2. (30 points) For the input impedance

$$z_{in}(s) = \frac{4(s+1)(s+3)}{(s+2)(s+5)}$$

- a) Find the zeros of its even part.
- b) Using  $k$  with positive real parts that are zeros of this even part, give a cascade synthesis of this input impedance using only passive elements.
- c) Discuss the effect of using  $k$  with negative real parts instead.

3. Extra credit (10 points max):

a) Give the reason why there are enough real positive zeros of the even part for the input impedance of 2. to be fully synthesized by a cascade of two of the 2-ports in 1 and a resistive load.

b) Prove that by extracting the 2-port of 1. from a real rational  $z_{in}$  the even part zeros of  $z_L$  are contained in the even part zeros of  $z_{in}$ .