

1. Point out those functions which are positive real; specify your reasons. Also point out those which are reactance functions if they exist.

$$(1) y(s) = \frac{s + 2}{s^3 + s^2 + 3s + 12}$$

$$(2) z(s) = \frac{s^2 - 5s + 7}{s^3 + s^2 + 3s + 12}$$

$$(3) y(s) = \frac{s^2 + 6s - 7}{s^3 - s^2 + 3s - 3}$$

$$(4) z(s) = \frac{s + 7}{s^4 + 5s^2}$$

$$(5) y(s) = \frac{s^3 + 5s + 7}{s^4 + 12s^2 + 36}$$

$$(6) z(s) = \frac{s^3 + 5s}{s^2 + 12s + 7}$$

$$(7) y(s) = \frac{s^2 + 7}{s^2 + 12s + 7}$$

$$(8) z(s) = \frac{s^2 + 7}{s^3 + 9s}$$

2. For those reactance functions in the above problem, synthesize them by the 1st and 2nd Cauer methods.
3. Determine the values of a for which the following is a positive real function. Among those determine a for y(s) to be an RC driving point admittance and for these a synthesize the following function as the driving-point admittance of an RC network using the 2nd Foster realization.

$$y(s) = \frac{s(s + 3)(s + 8)}{(s + 2)(s + a)}$$