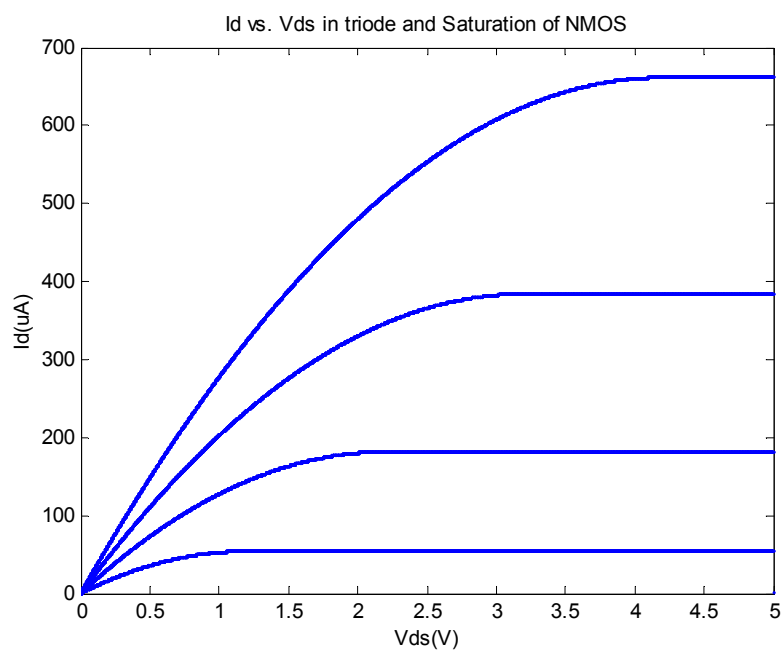


### Problem1

```
clear all
L=2;
W=3;
VTO=0.8;
KPn=50;

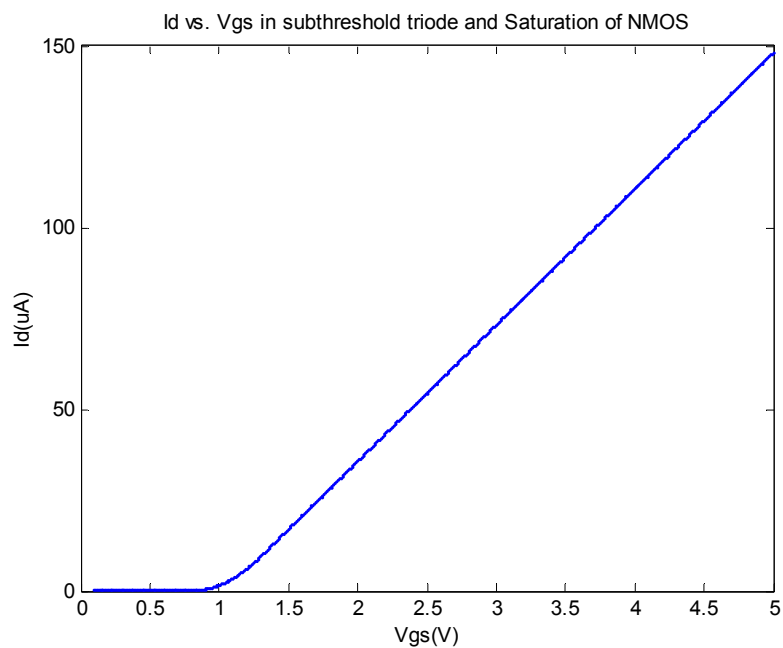
Vthn=VTO;
Vds=0.5;
for Vgs=0.1:0.01:5;
    if (Vgs-Vthn)>0
        if (Vds<=(Vgs-Vthn))
            Id=KPn*(W/L)*((Vgs-Vthn)*Vds-Vds*Vds/2);
        else
            Id=KPn/2*(W/L)*(Vgs-Vthn)^2;
        end
    else
        Id0=KPn*0.0259*0.0259*exp(1.8);
        Id=Id0*(W/L)*exp((Vgs-Vthn)/0.0259);
    end
    semilogy(Vgs,Id);
    hold on
end
xlabel('Vgs(V)');
ylabel('log Id(uA)');
title('log Id vs. Vgs in subthreshold triode and Saturation of NMOS')
```



### Problem 2:

```
clear all
L=2;
W=3;
VTO=0.8;
KPn=50;

Vthn=VTO;
Vds=0.5;
for Vgs=0.1:0.01:5;
    if (Vgs-Vthn)>0
        if (Vds<=(Vgs-Vthn))
            Id=KPn*(W/L)*((Vgs-Vthn)*Vds-Vds*Vds/2);
        else
            Id=KPn/2*(W/L)*(Vgs-Vthn)^2;
        end
    else
        Id0=KPn*0.0259*0.0259*exp(1.8);
        Id=Id0*(W/L)*exp((Vgs-Vthn)/0.0259);
    end
    plot(Vgs,Id);
    hold on
end
xlabel('Vgs(V)');
ylabel('Id(uA)');
title('Id vs. Vgs in subthreshold triode and Saturation of NMOS')
```



### Problem 6.5

The drive current of a short-channel MOSFET is given by Eq. (6.41)

$$\begin{aligned} I_{drive} &= v_{sat} \times C'_{ox} \times (V_{GS} - V_{THN} - V_{DS,sat}), \\ C'_{ox} &= \epsilon_{ox} / TOX = (8.85 \times 3.97 \text{ aF}/\mu\text{m}) / (75 \times 10^{-10} \text{ m}) = 4.685 \text{ fF}/\mu\text{m}^2 \\ I_{drive} &= 10^7 \text{ cm/s} \times 4.685 \text{ fF}/\mu\text{m}^2 \times (2.5 - .5 - 1.5) \text{ V} = \underline{234.25 \mu\text{A}/\mu\text{m}} \end{aligned}$$

For the long channel MOSFET in chapter five, we assume that electron mobility  $\mu$  does not vary with  $V_{DS}$ . For short-channel MOSFETs,  $V_{DS,sat}$  is not directly dependent on the  $V_{GS}$  and  $V_{TH}$ , but it is used to change the drift velocity. From figure 6.8 and Eq. (6.39), the  $V_{DS,sat}$  is dependent directly on the critical electrical field which causes the drift velocity to  $v_{sat}$ . Therefore,  $V_{DS,sat}$  is not equal to  $V_{GS} - V_{THN}$  for short-channel MOSFETs.

### Problem 6.7

From eq. (6.21), the output resistance is given by  $r_o = 1/(\lambda \cdot I_D)$ . Using level 1 MOSFET SPICE model, in saturation region,  $I_D = \text{MUZ} \cdot C_{ox} \cdot W \cdot (V_{GS} - V_{THN})^2 / 2L$

Therefore,

$$r_o = 2L / [\lambda \cdot \text{MUZ} \cdot C_{ox} \cdot W \cdot (V_{GS} - V_{THN})^2]$$

Set  $K = 2 / [\text{MUZ} \cdot C_{ox} \cdot W \cdot (V_{GS} - V_{THN})^2]$ ,

$$r_o = L / (\lambda \cdot K)$$

For  $10\mu\text{m}/2\mu\text{m}$  MOSFET, the effective resistance of NMOS is  $R_n = 12\text{k}\Omega \times 2/10 = 2.4\text{k}\Omega$ , and for the PMOS,  $R_p = 36\text{k}\Omega \times 0.2 = 7.2\text{k}\Omega$ . The capacitance between drain to ground is same for both NMOS and PMOS and equal to  $C_{ox} + 150\text{fF} = 166\text{fF}$ . From eq. (10.8) and (10.9), for NMOS,

$$t_{p,III} = 2.4\text{k}\Omega \times 166\text{fF} \approx \underline{398\text{ps}}, \quad t_{r,III} = 2 \times 2.4\text{k}\Omega \times 166\text{fF} \approx \underline{797\text{ps}}$$

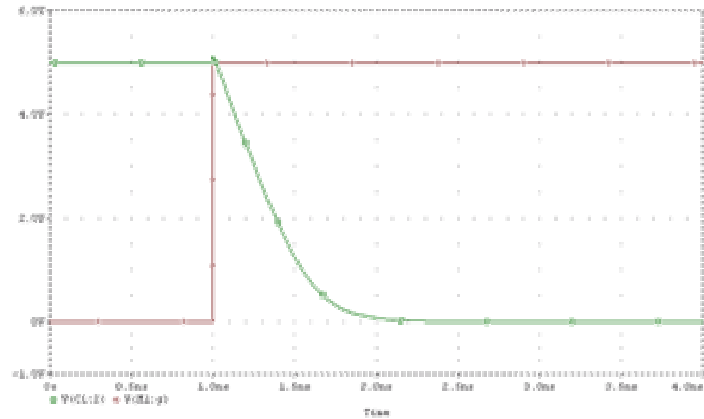
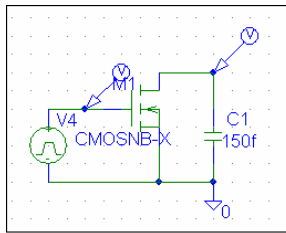
for PMOS,

$$t_{p,II} = 7.2\text{k}\Omega \times 166\text{fF} \approx \underline{1.2\text{ns}}, \quad t_{r,II} = 2 \times 7.2\text{k}\Omega \times 166\text{fF} \approx \underline{2.4\text{ns}}$$

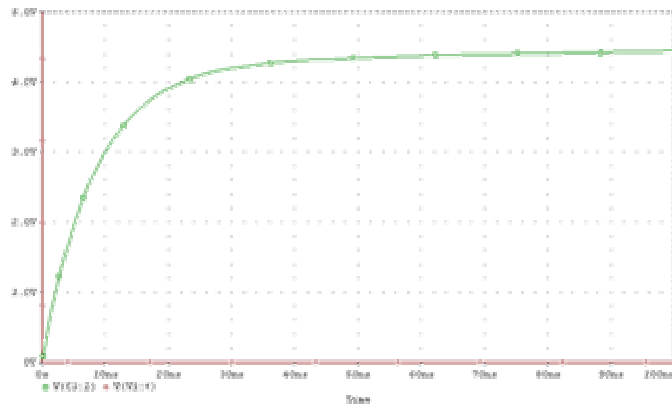
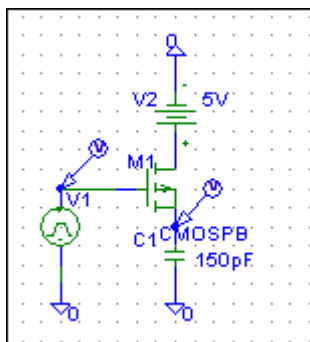
Simulation:

Trick: need to set the IC value for the Capacitor.

## NMOS



## PMOS



### Problem 10.7

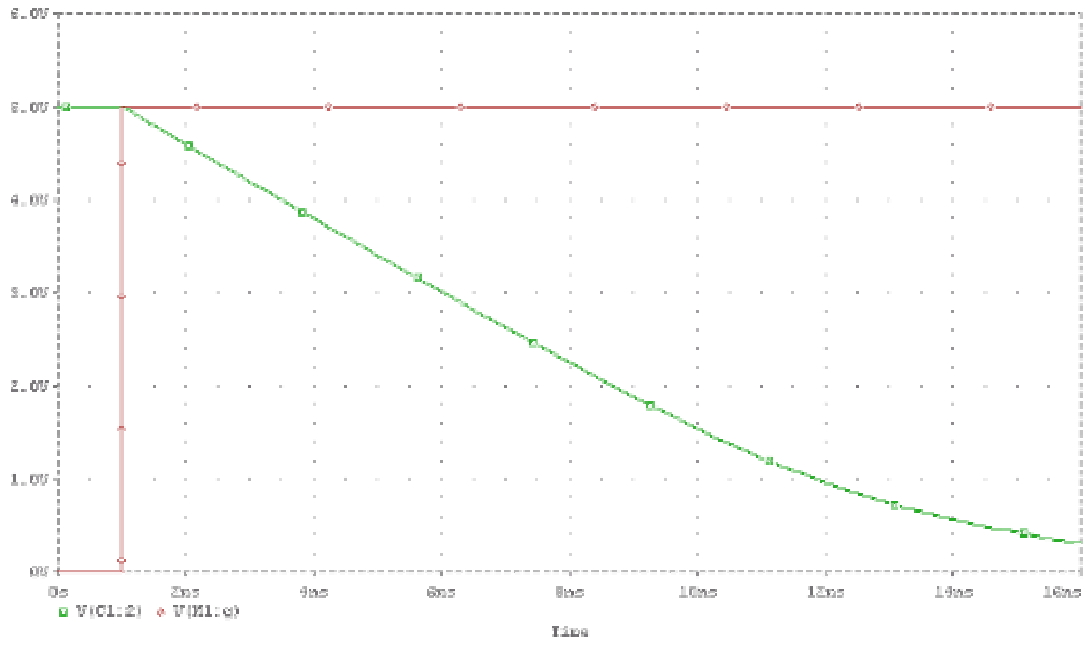
For  $3\mu\text{m}/2\mu\text{m}$  MOSFET, the effective resistance of NMOS is  $R_n = 12\text{k}\Omega \times 2/3 = 8\text{k}\Omega$ , and for the PMOS,  $R_p = 24\text{k}\Omega$ : The capacitance between drain to ground is same for both NMOS and PMOS and equal to  $C_{ox} + 1\text{pF} \approx 1\text{pF}$ . From eq. (10.8) and (10.9), for NMOS,

$$t_{pHL} = 8\text{k}\Omega \times 1\text{pF} = \underline{8\text{ns}}, \quad t_{HL} = 2 \times 8\text{k}\Omega \times 1\text{pF} = \underline{16\text{ns}}$$

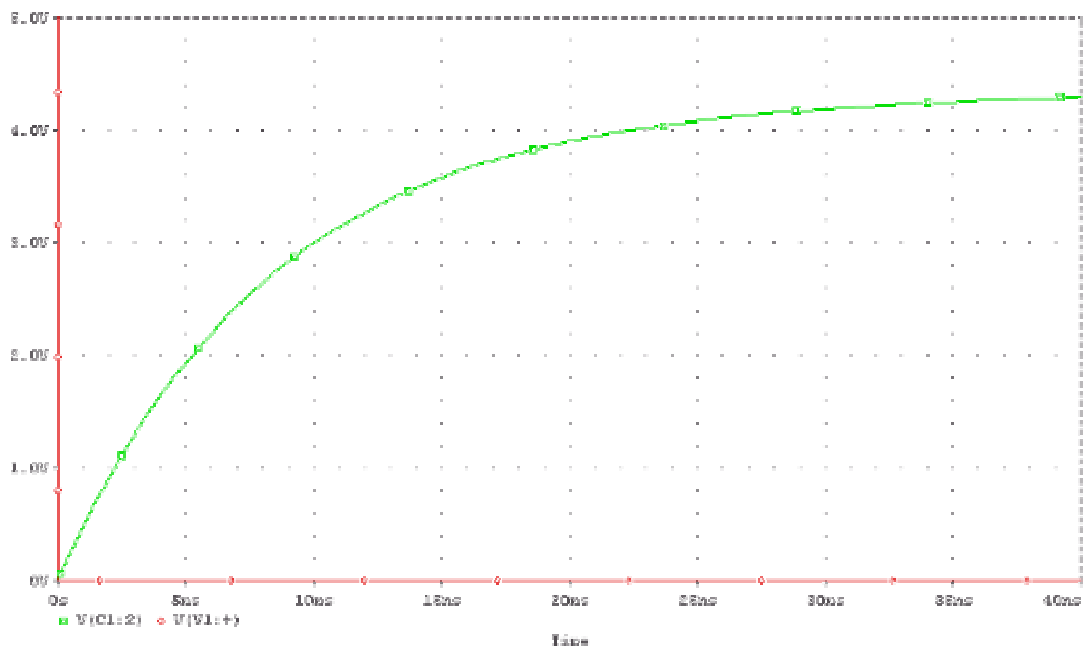
for PMOS,

$$t_{pLH} = 24\text{k}\Omega \times 1\text{pF} = \underline{24\text{ns}}, \quad t_{LH} = 2 \times 24\text{k}\Omega \times 1\text{pF} = \underline{48\text{ns}}$$

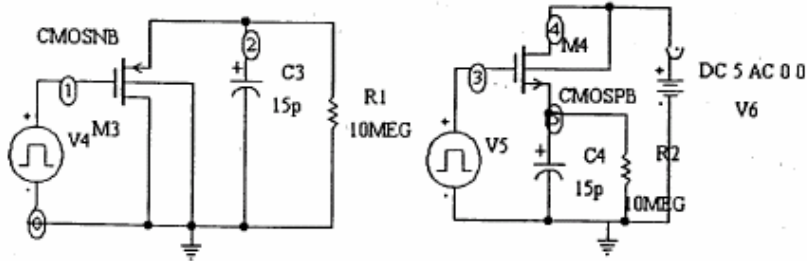
NMOS:



PMOS:



**Problem 10.8**



For nmos,  $t_{pHL} \approx 8k\Omega \times 15pF = 120ns$ ; for pmos,  $t_{pLH} \approx 360ns$

