#### Introduction to Cryptology

Lecture 10

#### Announcements

- HW4 due Tuesday, 3/6
- Extra Class Exercise and Solution on Course Webpage (on PRFs)

## Agenda

- Last time:
  - CPA-secure encryption from PRF (K/L 3.5)
- This time:
  - PRP (Block Ciphers) (K/L 3.5)
  - Modes of operation (K/L 3.6)
  - New topic:
    - Message Authentication Codes (MAC) (K/L 4.2)

### Block Ciphers/Pseudorandom Permutations

Definition: Pseudorandom Permutation is exactly the same as a Pseudorandom Function, except for every key k,  $F_k$  must be a permutation and it must be indistinguishable from a random permutation.

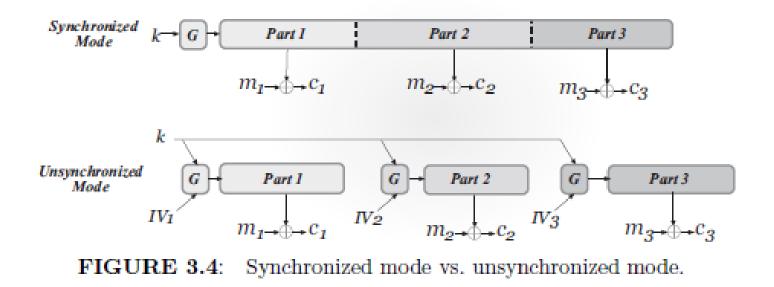
## **Strong Pseudorandom Permutation**

Definition: Let  $F: \{0,1\}^* \times \{0,1\}^* \rightarrow \{0,1\}^*$  be an efficient, length-preserving, keyed permutation. We say that F is a strong pseudorandom permutation if for all ppt distinguishers D, there exists a negligible function negl such that:

$$|\Pr[D^{F_k(\cdot),F^{-1}_k(\cdot)}(1^n) = 1] - \Pr[D^{f(\cdot),f^{-1}(\cdot)}(1^n) = 1]| \le negl(n).$$

where  $k \leftarrow \{0,1\}^n$  is chosen uniformly at random and f is chosen uniformly at random from the set of all permutations mapping n-bit strings to n-bit strings.

#### Modes of Operation—Stream Cipher



# If sender and receiver are willing to maintain state, can encrypt multiple messages.

#### Modes of Operation—Block Cipher

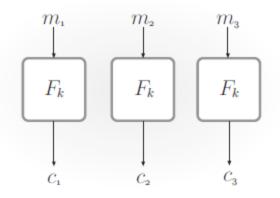


FIGURE 3.5: Electronic Code Book (ECB) mode.

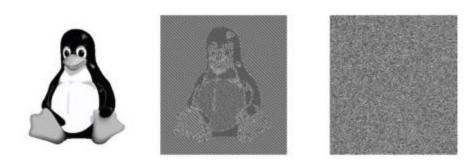


FIGURE 3.6: An illustration of the dangers of using ECB mode. The middle figure is an encryption of the image on the left using ECB mode; the figure on the right is an encryption of the same image using a secure mode.

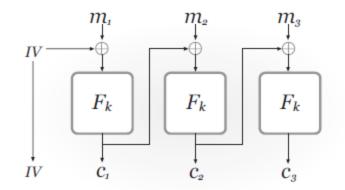


FIGURE 3.7: Cipher Block Chaining (CBC) mode.

#### Modes of Operation—Block Cipher

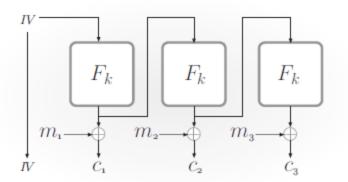


FIGURE 3.9: Output Feedback (OFB) mode.

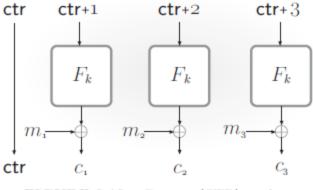


FIGURE 3.10: Counter (CTR) mode.

### Message Integrity

• Secrecy vs. Integrity

• Encryption vs. Message Authentication

## Message Authentication Codes

Definition: A message authentication code (MAC) consists of three probabilistic polynomial-time algorithms (Gen, Mac, Vrfy) such that:

- 1. The key-generation algorithm *Gen* takes as input the security parameter  $1^n$  and outputs a key k with  $|k| \ge n$ .
- 2. The tag-generation algorithm Mac takes as input a key k and a message  $m \in \{0,1\}^*$ , and outputs a tag t.  $t \leftarrow Mac_k(m)$ .
- 3. The deterministic verification algorithm Vrfy takes as input a key k, a message m, and a tag t. It outputs a bit bwith b = 1 meaning valid and b = 0 meaning invalid.  $b \coloneqq Vrfy_k(m, t)$ .

It is required that for every n, every key k output by  $Gen(1^n)$ , and every  $m \in \{0,1\}^*$ , it holds that  $Vrfy_k(m, Mac_k(m)) = 1$ .

# Security of MACs

The message authentication experiment  $MACforge_{A,\Pi}(n)$ :

- 1. A key k is generated by running  $Gen(1^n)$ .
- 2. The adversary A is given input  $1^n$  and oracle access to  $Mac_k(\cdot)$ . The adversary eventually outputs (m, t). Let Q denote the set of all queries that A asked its oracle.
- 3. A succeeds if and only if (1)  $Vrfy_k(m,t) = 1$ and (2)  $m \notin Q$ . In that case, the output of the experiment is defined to be 1.

## Security of MACs

Definition: A message authentication code  $\Pi = (Gen, Mac, Vrfy)$  is existentially unforgeable under an adaptive chosen message attack if for all probabilistic polynomial-time adversaries A, there is a negligible function neg such that:

 $\Pr[MACforge_{A,\Pi}(n) = 1] \le neg(n).$