

ENEE 222: 4/09 Class

Material: Lecture videos 16.2, 17.1, 17.2, 17.3

1. Suppose the DFT of the vector

$$[a \quad b \quad c \quad d]^T$$

contains no zero entries. Which (one or more) of the following vectors \mathbf{x} is certain to have *exactly* four nonzero entries in its DFT \mathbf{X} ?

A. $\mathbf{x} = [a \quad b \quad c \quad d \quad a \quad b]^T$

B. $\mathbf{x} = [a \quad b \quad c \quad d \quad a \quad b \quad c \quad d]^T$

C. $\mathbf{x} = [a \quad b \quad c \quad d \quad a \quad b \quad c \quad d \quad a \quad b]^T$

D. $\mathbf{x} = [a \quad b \quad c \quad d \quad a \quad b \quad c \quad d \quad a \quad b \quad c \quad d \quad a \quad b \quad c \quad d]^T$

2. If

$$\mathbf{x} = [a \quad b \quad c \quad 0 \quad 0 \quad 0 \quad 0 \quad 0 \quad 0 \quad 0 \quad 0 \quad 0]^T$$

has DFT

$$\mathbf{X} = [X_0 \quad X_1 \quad X_2 \quad X_3 \quad X_4 \quad X_5 \quad X_6 \quad X_7 \quad X_8 \quad X_9 \quad X_{10} \quad X_{11}]^T,$$

then the DFT of $[a \quad 0 \quad c \quad b]^T$ is given by

A. $[X_0 \quad X_3 \quad X_2 \quad X_1]^T$

B. $[X_0 \quad 0 \quad X_2 \quad X_1]^T$

C. $[X_0 \quad X_3 \quad X_6 \quad X_9]^T$

D. $[X_0 \quad X_9 \quad X_6 \quad X_3]^T$

3. $\mathbf{x} = \text{rand}(5,1)$;
 DFT1 = `fft(x,12)` ;
 DFT2 = `fft(x,32)` ;

What is the smallest value of N such that

$$\text{DFT3} = \text{fft}(\mathbf{x},N)$$

contains DFT1 and DFT2 as subvectors?

- A. N = 44 B. N = 96 C. N = 189 D. N = 384

4. The continuous-time signal

$$s(t) = 3 \cos(40\pi t + 0.8) + 5 \cos(96\pi t - 1.7)$$

is sampled at a rate $f_s = 160$ samples/sec. The DFT \mathbf{S} of the sample vector $\mathbf{s} = s[0 : L - 1]$ is then computed.

What is the smallest value of L (> 4) such that \mathbf{S} contains exactly four nonzero entries?

- A. $L = 20$ B. $L = 40$ C. $L = 48$ D. $L = 96$

5. (HW 20 i ii) The signal

$$\mathbf{x} = [a \ b \ c \ 0 \ 0 \ 0 \ a \ b \ c \ 0 \ 0 \ 0]^T$$

has DFT \mathbf{X} given by

$$\mathbf{X} = [D_0 \ D_1 \ D_2 \ D_3 \ D_4 \ D_5 \ D_6 \ D_7 \ D_8 \ D_9 \ D_{10} \ D_{11}]^T$$

If $\mathbf{x}^{(1)} = [a \ b \ c]^T$, express the DFT $\mathbf{X}^{(1)}$ in terms of nonzero D_k 's.

6. (HW 20 v) (Cont.) If the *time-domain* signal $\mathbf{x}^{(4)}$ has DFT

$$\mathbf{X}^{(4)} = [0 \ 0 \ 0 \ a \ b \ c]^T,$$

express the entries of $\mathbf{x}^{(4)}$ in terms of nonzero D_k 's.

7. (HW 21 iii) Let $\mathbf{s} = s[0 : 111]$, where

$$s[n] = A_1 \cos\left(\frac{3\pi n}{14} + \phi_1\right) + A_2 \cos\left(\frac{5\pi n}{8} - \phi_2\right)$$

Sketch the DFT magnitude $|S[k]|$ and phase $\angle S[k]$ against frequency index k .