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- Magnitude and phase spectra; symmetries
- Synthesis of a real-valued signal using its magnitude and phase spectra

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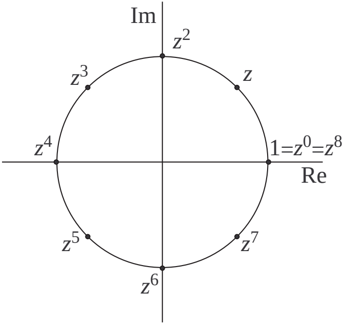

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