Consider the problem of finding a time familion x(t) such that x(0) = 1and X (277) = 0 and the functional is to be minimized. Use optimal control theory to solve this problem. 2. (Here time horizon refers to T) Consider the scaler system & = u. It is desired to find a feedback control law for u (-> such that the state x is segulated around a constant level 8. Determine such a feedback law by minimizing) (u²(+) + (x(+)-2)²) dt. Does the chaice of time horizon matter.

Consider the optimal control problem Min J[u] = [[x(+) L (+) x(+) + u(+) u(+)] d+ + (x(t)) -d) Q (x(t))-d) Subject to $\dot{x}(t) = A(t)x(t) + B(t)x(t)$ x (to) = x. Here X, L=L, A, B, Q and d are given. Show that the optimal control has the (K(t) x(t) + \frac{1}{2}\(\psi(t)\) where K and y satisfy suitable hypotheses, and state these hypotheses clearly. Hint: Invent a path-independence lemma that applies to linear forms in x, and use it in addition to the familiar one for quadratic forms.